



Subject: Introduction to
Derivatives and
Financial Markets

Chapter:

Category: Assignment
1 solutions

1. Answer : c

2. Answer : c

3. Answer: d

4. Answer: c

5. Answer: c

6. Answer: c

7. Answer: b

8. Answer: b

9. Answer: b

Answer: B

An investor who buys (has a long position) has a gain when a futures price increases. An investor who sells (has a short position) has a loss when a futures price increases.

10. Answer: c

Answer: C

Suppose that S_T is the final asset price and K is the strike price/forward price. A short forward contract leads to a payoff of $K - S_T$. A long position in a European call option leads to a payoff of $\max(S_T - K, 0)$. When added together we see that the total position leads to a payoff of $\max(0, K - S_T)$, which is the payoff from a long position in a put option. C can also be seen to be true by plotting the payoffs as a function of the final stock price.

11. Answer: b

Answer: B

One futures contract protects a portfolio worth 1250×250 . The number of contract required is therefore $3,000,000 / (1250 \times 250) = 16$. To remove market risk we need to gain on the contracts when the market declines. A short futures position is therefore required.

12. Answer: d

Answer: D

There will be a margin call when more than \$1000 has been lost from the margin account so that the balance in the account is below the maintenance margin level. Because the company is short, each one cent rise in the price leads to a loss of $0.01 \times 50,000$ or \$500. A greater than 2 cent rise in the futures price will therefore lead to a margin call. The future price is currently 70 cents. When the price rises above 72 cents there will be a margin call.

13. Answer: a

The optimal hedge ratio is

$$0.7 \times \frac{1.2}{1.4} = 0.6$$

The beef producer requires a long position in $200000 \times 0.6 = 120,000$ pounds of cattle. The beef producer should therefore take a long position in 3 December contracts closing out the position on November 15.

14. Answer: d

A short position in

$$1.3 \times \frac{50,000 \times 30}{50 \times 1,500} = 26$$

contracts is required. It will be profitable if the stock outperforms the market in the sense that its return is greater than that predicted by the capital asset pricing model.

15.

- The minimum variance hedge ratio is $0.95 \times 0.43 / 0.40 = 1.02125$.
- The hedger should take a short position.
- The optimal number of contracts when daily settlement is not considered is $1.02125 \times 55,000 / 5,000 = 11.23$ (or 11 when rounded to the nearest whole number)
- The optimal number of contracts is $\hat{\rho} \hat{\sigma}_S V_A / (\hat{\sigma}_F V_F)$ where $\hat{\rho}$ is correlation between percentage one-day returns of spot and futures, $\hat{\sigma}_S$ and $\hat{\sigma}_F$ are the standard deviations of percentage one-day returns on spot and futures, V_A is the value of the position and V_F is the futures price times the size of one contract. In this case $V_A = 55,000 \times 28 = 1,540,000$ and $V_F = 5,000 \times 27 = 135,000$. If we assume that $\hat{\rho} = 0.95$

and $\hat{\sigma}_S / \hat{\sigma}_F = 0.43 / 0.40 = 1.075$, the optimal number of contracts when daily settlement is considered $0.95 \times 1.075 \times 1,540,000 / 135,000 = 11.64$ (or 12 when rounded to the nearest whole number).



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