

Subject: Numerical methods and algebra

Chapter: Unit 1 & 2

Category: Assignment 1

## IACS

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- 1. The radius of a circular plate is measured as 12.65 cm instead of the actual length 12.5 cm. find the following in calculating the area of the circular plate:
- (i) Absolute error (ii) Relative error (iii) Percentage error
- 2. The following logarithmic table is given

X	f(x) = log(x)
4.0	0.60206
4.5	0.6532125
5.5	0.7403627
6.0	0.7781513

- (a) Interpolate log (5) using the points x=4 and x=6
- (b) Interpolate  $\log$  (5) using the points x=4.5 and x=5.5
- 3. Find the root of  $x^4$ -x-10 = 0 approximately upto 5 iterations using Bisection Method. Let a = 1.5 and b = 2.
- 4. Find a root of an equation  $f(x)=x^3-x-1$  using Newton Raphson method
- 5. If A is a square matrix such that  $A^2=A$ , then find the value of  $7A-(I+A)^3$ , here I is an identity matrix.
- 6. Find out the inverse of  $A = \begin{bmatrix} 1 & -1 & 2 \\ 4 & 0 & 6 \\ 0 & 1 & -1 \end{bmatrix}$  using elementary row transformations.
- 7. Sabrina walked 75 meters to the east. Then she turned 30 degrees to the left and walked 25 meters. Determine the magnitude of Sabrina's displacement vector.
- 8. Find all eigenvalues and corresponding eigenvectors for the matrix A if

$$\begin{pmatrix}
2 & -3 & 0 \\
2 & -5 & 0 \\
0 & 0 & 3
\end{pmatrix}$$



- 9. Use Newton's Method to determine  $x_2$  for  $f(x) = x^3 7x^2 + 8x 3$  if  $x_0 = 5$
- 10. Find the approximated value of x till 4 iterations for  $e^{-x} = 3 \log(x)$  using Bisection Method.

11. If 
$$A = \begin{bmatrix} a & 0 & 0 \\ 0 & a & 0 \\ 0 & 0 & a \end{bmatrix}$$
 then find the value of |adj A|

12. If 
$$\begin{bmatrix} 1 & x & 1 \end{bmatrix} \begin{bmatrix} 1 & 3 & 2 \\ 0 & 5 & 1 \\ 0 & 3 & 2 \end{bmatrix} \begin{bmatrix} x \\ 1 \\ -2 \end{bmatrix} = 0$$
. Then find the value of x.

13. If 
$$A = \begin{bmatrix} 1 & 0 & 0 \\ 3 & 5 & 0 \\ 2 & 1 & 8 \end{bmatrix}$$
 then find the inverse of the matrix using the adjoint method.

14. Construct the matrix  $A = [a_{ij}]_{3x3}$ , where  $a_{ij} = i - j$ . State whether A is symmetric or skew-symmetric.