

Probability & Stats. Assignment - II

Q1. (a.) $\sum x^2 = 928000$ $\sum x = 850$
 $\sum y^2 = 372717$ $\sum y = 1737$
 $\sum xy = 1825600$

$S_{xx} = 852750$
 $S_{yy} = 71000$
 $S_{xy} = 34915$

$B = 0.040944$

$K = 170.219$

$\therefore Eq^{th} = K + Bx$
 $= 170.219 + 0.040944x$

(b.) $\therefore B = 0.040944$

i.e., B is close to 0

Hence, it is not significant

Q2. (i.) $\sum x^2 = 12666.58$ $\sum x = 385.2$
 $\sum y^2 = 119026.9$ $\sum y = 1162.5$
 $\sum xy = 38191.41$

$S_{xx} = 901.66$
 $S_{yy} = 875.16$
 $S_{xy} = 6409.7125$

$B = 2.9011$

$K = 3.7496$

$\therefore Eq^{th} = 3.7496 + 2.9011x$

$$(ii) \sigma^2 = 387.0744$$

$$\hat{\beta} \sim N(\beta, \sigma^2/S_{xx})$$

95% C.I.

$$= \beta \pm t_{2.5\%, 12} \left(\frac{\sigma}{\sqrt{S_{xx}}} \right)$$

$$= 2.9011 \pm (2.228)(1.182)$$

$$= (0.379, 5.423)$$

$$(iii) Y \sim N(\alpha + \beta x, \frac{1}{n} + \frac{(x - \bar{x})^2}{S_{xx}} \sigma^2)$$

~~Residuals~~

$$C.I. = \mu_0 \pm t_{\alpha/2, n-2} \sqrt{\left(\frac{1}{n} + \frac{(x_0 - \bar{x})^2}{S_{xx}} \right) \sigma^2}$$

$$= 119.7936 \pm 22.143$$

$$= (97.6504, 141.93)$$

Q8. (i) In city A & city B, it takes longer while travelling in peak hours. While in city C the time diff. is similar where as in city D, we might reach early.

$$\underline{Q6.} \quad \sum x = 39$$

$$\sum y = 562$$

$$\sum x^2 = 207$$

$$\sum y^2 = 40508$$

$$\sum xy = 2853$$

$$S_{xx} = 54.9$$

$$S_{yy} = 8923.6$$

$$S_{xy} = 661.2$$

$$(i.) r = \frac{S_{xy}}{\sqrt{S_{xx} \cdot S_{yy}}} = 0.944662$$

$$(ii.) \beta = 12.0437$$

$$\alpha = 9.22957$$

$$\therefore \text{Eq}^n = 9.22957 + 12.0437x$$

$$(iii.) SS_{TOT} = SS_{REG} + SS_{RES}$$

$$SS_{RES} = \frac{S^2_{xy}}{S_{xx}} = 7963.30$$

$$SS_{RES} = S_{yy} - \frac{S^2_{xy}}{S_{xx}} = 960.295$$

$$\therefore SS_{TOT} = 7963.30 + 960.295$$

$$= 8923.595$$

$$(iv.) R^2 = \frac{S^2_{xy}}{S_{xx} \cdot S_{yy}} = R^2 \text{ ~~0.8923~~ } = 0.8923$$

$$\underline{Q7:} \quad \sum x^2 = 7545.90$$

$$\sum x = 174.13$$

$$\sum y^2 = 4747.45$$

$$\sum y = 187.84$$

$$S_{xy} = 2176.24$$

$$S_{xx} = 4789.421$$

$$S_{yy} = 1189.2079$$

$$(i.) \beta = \frac{S_{xy}}{S_{xx}} = 2.20017$$

$$\alpha = -16.8432$$

$$\hat{y} = -16.8432 + 2.20017x$$

(ii) $H_0: \beta = 0$ V/S $H_1: \beta \neq 0$

$$\sigma^2 = 139.8121$$

$$t_{\text{cal}} = \frac{\hat{\beta} - \beta}{\sigma / \sqrt{S_{xx}}} = 10.77176$$

$$t_{\text{tab}} = 2.776$$

$$t_{\text{cal}} > t_{\text{tab}}$$

$\therefore$ Reject H_0

$\therefore$ There is linear relationship between X & Y .

(iii) $r = \frac{S_{xy}}{\sqrt{S_{xx} \cdot S_{yy}}} = \cancel{0.912128} 0.912128$

Q9. $\sum x^2 = 277.5$ $\sum x = 45$
 $\sum y^2 = 43956$ $\sum y = 644$
 $\sum xy = 2602$

$$S_{xx} = 75$$

$$S_{yy} = 2482.4$$

$$S_{xy} = -296$$

(i) Looking at the plot, a negative correlation between X & Y can be seen.

(ii) $r = \frac{S_{xy}}{\sqrt{S_{xx} \cdot S_{yy}}} = -0.686$

$\therefore$ There is a strong negative correlation.

(iii.) $\tanh^{-1} r \sim N(\tanh^{-1} \rho, \frac{1}{n-3})$
 $H_0: \rho = 0$ v/s $H_1: \rho < 0$

$$Z_{cal} = \frac{\tanh^{-1} r - \tanh^{-1} \rho}{\sqrt{\frac{1}{n-3}}} = \frac{-0.84036 - 0}{\sqrt{\frac{1}{810-3}}}$$

$$= -2.22338$$

$Z_{tab} \Rightarrow \pm 1.96 = Z_{2.5\%}$
 $\Rightarrow \pm 2.5758 = Z_{0.5\%}$

$\therefore$ at 5% level of significance, we reject H_0 .
 $\therefore$ We do not reject H_0 at 1% level of significance.

$\Rightarrow$ There is a negative correlation at 5% level of significance.

$\Rightarrow$ There is no correlation at 1% level of significance.

Notes:-

Doubts = Q3, Q4, Q5, Q8, Q10