

①

FM Assignment-2

$$1) \text{ loan} = ₹20,000$$

$$\text{Monthly instalment} = 427.9$$

$$\text{Yrly instalment} = 427.9 \times 12 \\ = 5134.8$$

$$i) 20000 = 5134.8 a_{\overline{5}|i}^{(12)}$$

$$\frac{1 - (1+i)^{-5}}{12((1+i)^{1/12} - 1)} = 3.894991$$

$$\Rightarrow i = 10.80\% \rightarrow \text{APR}$$

$$ii) \text{ Loan left} = 20000 - 5134.8 \\ = 14865.2$$

$$i = 10.80\%$$

$$\text{Monthly } I = 274.49$$

$$\text{Yrly } I = 3293.88$$

$$14865.2 = 3293.88 \times a_{\overline{n}|i}^{(12)}$$

$$\frac{1 - (1.108)^{-n}}{0.1029961} = 4.5129756$$

$$(1.108)^{-n}$$

②

ii) Loan left after 1st payment

$$20000(1.1080)^1 - 5134.85$$

$$20000(1.1080) - 5134.85 \left[\frac{(1.1080)^1 - 1}{0.1080} \right]$$

$$= 22158.892$$

$$\rightarrow \text{Yrly I} = 274.49 \times 12$$

$$22158.892 = 3293.88 \dot{a}_{\overline{n}|i} = 3293.88$$

$$6.7272192 = \frac{1 - (1.080)^n}{12[(1.080)^n - 1]}$$

$$(1.080)^n = 0.4805968$$

$$n = 9.5207466 \text{ yrs}$$

$$\rightarrow \text{Term of Total Loan} = 10.5207466$$

$$\text{iii) Interest of Og. loan} = 5134.8 \times 5 - 20000 = 5675$$

$$\begin{aligned} \text{Interest of New Loan} &= 513.48 \times 1 + 3293.88 \times 9.5207466 \\ &\quad - 2000 \\ &= 16494.99681 \end{aligned}$$

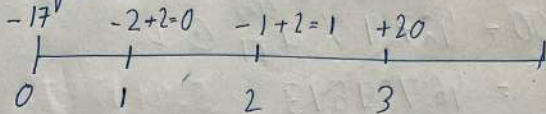
$$\begin{aligned} \text{New Interest on reconstructed loan} &= 16494.99681 - 5675 \\ &= 10819.99681 \end{aligned}$$

~~Interest is paid more in original loan by
 $\Rightarrow 464.871209$~~

- 3)
- 2) i) a) Discounted Payback Period - The amount of time it takes for the initial cost of a project to equal to discounted value of expected cash flows, or the time it takes to break even for an investment, considering the time value of money.
- b) The Payback Period - The time required to recover the funds expended in an investment, or to reach break even point without discounting cashflows.

ii) ~~The~~ Payback Period doesn't account for time value of money and therefore discounted payback period is more accurate

iii) Project A $\rightarrow$



$$i) NPV_A = -17 + 1v^2 + 20v^3 = 0$$

$$-17 + 1(1+i)^{-2} + (1+i)^{-3} \times 20 = 0$$

$$i = 7\%$$

$$LHS = 0.1993$$

$$i = 8\%$$

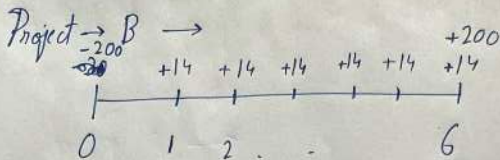
$$LHS = -0.266$$

Using interpolation $\rightarrow$

$$i + \frac{y - y_1}{y_2 - y_1} = IRR_A \Rightarrow 7.4\%$$

$$\begin{aligned} ii) NPV_A &= -17 + (1.06)^{-2} + 20(1.06)^{-3} \\ &= 0.6823821 \times 10000 = 6823.821 \end{aligned}$$

⑤



$$NPV_B = 0 = -200 + 14[v + v^2 + v^3 + v^4 + v^5] + 214v^6$$

$$= -200 +$$

$$i = 6\%$$

$$LHS = 9.8346$$

$$i = 8\%$$

$$LHS = -9.245$$

Using interpolation

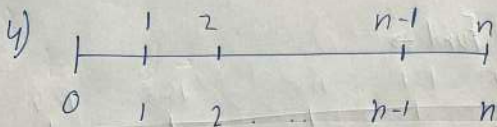
$$i = + \frac{y - y_1}{y_2 - y_1} \Rightarrow IRR_B = 7\%$$

$$NPV_B = -200 + 14 [(1.06)^{-1} + (1.06)^{-2} + (1.06)^{-3} + (1.06)^{-4} + (1.06)^{-5}] + 214(1.06)^{-6}$$

$$= 9.8346487 \times (1000) = 9834.6487$$

c) Minimum interest rate for A $\rightarrow$ 7.4%, B $\rightarrow$ 7%.
He could consider Discounted Payback Period.

⑧



$$PV_0 = 1 + 2v + 3v^2 + \dots + (n-1)v^{(n-1)} + nv^n \quad -i)$$

$$(1+i)(I_0)_{\overline{n}|} = 1 + 2v + 3v^2 + \dots + (n-1)v^{(n-2)} + nv^{n-1} \quad -ii)$$

ii) - i)

$$i(I_0)_{\overline{n}|} = 1 + v + v^2 + \dots + v^{n-1} - nv^n$$

$$(I_0)_{\overline{n}|} = \frac{\ddot{a}_{\overline{n}|} - nv^n}{i}$$



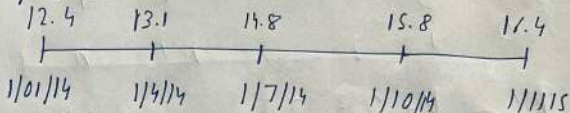
$$(I\ddot{o})_{\overline{n}|} = 1 + 2v + 3v^2 + \dots + nv^{n-1}$$

$$= (1+i)(I_0)_{\overline{n}|}$$

$$(I\ddot{o})_{\overline{n}|} = (1+i) \left(\frac{\ddot{a}_{\overline{n}|} - nv^n}{i} \right)$$

$$(I\ddot{o})_{\overline{n}|} = \frac{\ddot{a}_{\overline{n}|} - nv^n}{d}$$

9)

5) i) Property Fund $\rightarrow$ 

$$(1+i) = \frac{13.1}{12.4} \times \frac{14.8}{13.1} \times \frac{15.8}{14.8} \times \frac{16.4}{15.8}$$

$$1+i = \frac{16.4}{12.4} \Rightarrow i = 32.26\%$$

Equity Fund $\rightarrow$ 

$$1+i = \frac{15.5}{12.1} = 28.10\%$$

~~ii) a) Yield_{PF} = $\frac{16.4}{12.4} \rightarrow 32.26\%$~~

~~Yield_{EF} = $\frac{15.5}{12.1} \rightarrow 28.10\%$~~

~~b) Yield_{PF} = $\frac{13.1}{12.4} \times \frac{14.8}{13.1} \times \frac{15.8}{14.8} \times \frac{16.4}{15.8}$~~

~~$12.4X = 13.1Y = 14.8Z = 15.8A = 16.4B$~~

6) ⁽¹⁰⁾ Loan $\rightarrow 160000$, $i = 8\%$.

i) $160000 = X a_{\overline{10}|}$

$$\frac{160000}{1 - (1.08)^{-10}} \times 0.08 = X$$

$$X = 23,844.71819$$

ii) ~~$160000 - 23844.71819 \times$~~

Loan after 4th repayment $= 160000 (1+i)^4 - 23844.71819 S_{\overline{4}|}$

$$160000 (1.08)^4 - 23844.71819 X \left[\frac{(1.08)^4 - 1}{0.08} \right]$$

$$= 110231.2628$$

$$110231.2688 = X a_{\overline{6}|} @ 10\%$$

$$\frac{110231.2688 \times 0.1}{1 - (1.1)^{-6}} = X$$

$$X = 25309.91286$$

Loan after 7th Payment $\rightarrow$

iii) $\Rightarrow (110231.2628)(1+i)^3 - 25309.91286 X S_{\overline{3}|}$

$$110231.2628 (1.1)^3 - 25309.91286 \left[\frac{(1.1)^3 - 1}{0.1} \right]$$

$$\Rightarrow 62941.99921$$

$$62941.99921 = X a_{\overline{37}|0.09}$$

$$X = \frac{62941.99921}{1 - (1.09)^{-37}} \times 0.09$$

$$X = 24865.53622$$

Total $i = ?$

$$\cancel{160000} = 2486$$

$$\text{Average Installment} = \frac{23844.7182 \times 4 + 25309.9129 \times 3 + 24865.6362}{10}$$

$$= 24590.52202$$

$$160000 = 24590.52202 a_{\overline{10}|i} @ i$$

$$\frac{6.50657192}{\cancel{160000}} = \frac{1 - (1+i)^{-10}}{i}$$

$$i = 8.68\%$$

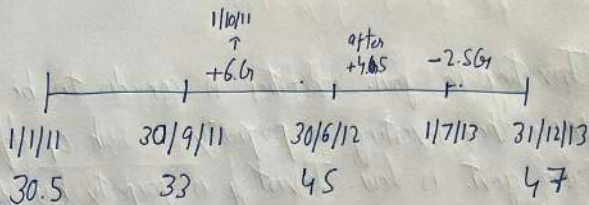
- 7) i) Investing in govt. securities is considered to be safer than investing in property as risk of default from govt. is low. Investing in property has various disadvantages as it requires costs of maintenance, tax etc and its value could decline or rent could drop.
- ii) a) Govt. invite bids for large projects that must be submitted within a finite deadline, ~~at~~^{up to} a particular price (considered lowest price) set by govt.

b)

8)

(13)

9)



$$(1+i)^3 = \frac{33}{30.5} \times \frac{45}{39} \times \frac{47}{48.57}$$

$$(1+i)^3 = 1.261847618 \quad 1.248423707$$

7.68%

$$i = \underline{\underline{8.0609972\%}} \quad (\text{TWRR})$$

$$\text{MWRR} = 30.5(1+i)^3 + 6(1+i)^{\frac{27}{12}} + 45(1+i)^{1.5} - 2.5(1+i)^{1.5} = 47$$

$$i = 7.2\%$$

ii) TWRR is better than MWRR because it takes interest with respect to time in account, whereas MWRR takes money into account, therefore when major chunk of money is used determines MWRR.

$$10) i = 12\%$$

$$\begin{aligned} \text{PV of Installments} &= 180000 a_{\overline{15}|} + 20000 (Ia)_{\overline{15}|} \\ &= 180000 \left(\frac{1 - (0.12)^{-15}}{0.12} \right) + 20000 \left(\frac{1 - (0.12)^{-15}}{0.12} \times 0.12 - 15 \times (0.12)^{-15} \right) \\ &= 1225955.608 + 814620.7282 \\ &= 2040576.326 \rightarrow \text{Loan} \end{aligned}$$

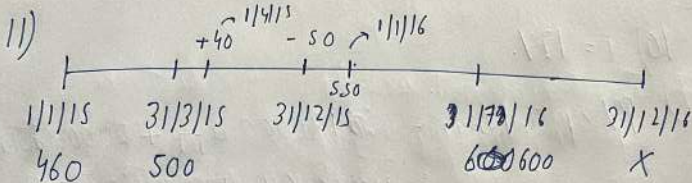
$$80\% \rightarrow 2040576.326$$

$$100\% \rightarrow \frac{2040576.326}{80} \times 100 = 2550720.408$$

↳ Total Cost

ii) ~~Loan at start of 9th yr~~ →

$$\begin{aligned} & \frac{(2040576.326)(1+i)^8}{1+i} - \\ \text{Loan at start of 9th yr} &= 340000 a_{\overline{7}|} + 20000 (Ia)_{\overline{7}|} \\ &= 340000 \times \left(\frac{1 - (0.12)^{-7}}{0.12} \right) \times 0.12 \\ & \quad + 20000 \left(\frac{(0.12)^{-7} \times 0.12 - 7 \times (0.12)^{-7}}{0.12} \right) \\ &= 19 \end{aligned}$$



$$i) TWRR \rightarrow (1+i)^2 = \frac{500}{460} \times \frac{500}{540} \times \frac{600}{550} \times \frac{X}{600}$$

$$i = 20\%$$

$$(1.2)^2 = 1.44$$

$$X = 786.9312$$

$$ii) MWRR = 460(1+i)^2 + 40(1+i)^{21/12} - 50(1+i)^1 = 786.9312$$

$$= 30.9\%$$

$$1^{st} Y_n \rightarrow 460(1+i_1) + 40(1+i_1)^{3/4} = 500$$

$$i_1 = 0\%$$

$$2^{nd} Y_n \rightarrow 550(1+i_2) = 786.9312$$

$$i_2 = 43.08\%$$

$$\text{Linked Internal Rate Return} = (1+i)^2 = 1 \times 1.4308$$

$$i = 19.62\%$$

13) Loan - 988000, $i = 7\%$.

$$i) 988000 = X a_{\overline{25}|}^{(12)}$$

$$X = \frac{988000}{1 - (1.07)^{-25}} \times 12 [(1.07)^{112} - 1]$$

$$X = 82176.50031$$

$$\text{Monthly Inst.} = \frac{X}{12} = 6848.041692$$

ii) Loan O/s after 138/12 payments $\rightarrow$

$$\frac{988000(1.07)^{138/12} - 82176.50031 [(1.07)^{138/12} - 1]}{0.07}$$

$$L_{138/12} = 82176.50031 a_{\overline{114/12}|}^{(12)}$$

$$= 82176.50031 \left[\frac{1 - (1.07)^{-136/12}}{12 [(1.07)^{112} - 1]} \right]$$

$$= 648575.4677$$

$$i) 988000 = X a_{\overline{25}|}$$

$$X = \frac{988000}{1 - (1.07)^{-25}} \times [12[(1.07)^{11\frac{1}{2}} - 1]]$$

$$X = 82176.50031$$

$$\text{Monthly } I = \frac{X}{12} = 6848.041692$$

ii)

ii) Loan O/s after $11\frac{1}{2}$ Yrs $\rightarrow$

$$\begin{aligned} \text{Loan O/s after } 11\frac{1}{2} \text{ Yrs} &= 82176.50031 a_{\overline{13\frac{10}{12}}|}^{(12)} \\ &= \frac{82176.50031 \times (1 - (1.07)^{-13\frac{10}{12}})}{12 [(1.07)^{11\frac{1}{2}} - 1]} \\ &= 736121.1001 \end{aligned}$$

$$\text{Int} = 736121.1001 \times \frac{i^{(12)}}{12} = 4162.136$$

$$\text{Capital} = 736121.1001 - 4162.136 = 731958.964$$

Installment b/w
 iv) ~~Loan~~ ~~at~~ ~~10th April/33~~ & ~~10th March/34~~

$$\text{Loan}_{17\frac{8}{12}} = X a_{\overline{7\frac{1}{12}}|i}^{(12)} \text{ \& } \text{Loan}_{18\frac{8}{12}} = X a_{\overline{6\frac{4}{12}}|i}^{(12)} - ii)$$

$$ii) - i) = 82176.50031 \times \left[\frac{1 - (1.07)^{\overline{76\frac{11}{12}} - 88\frac{1}{12}}}{12[(1.07)^{12} - 1]} \right] -$$

$$82176.50031 \times \left[\frac{1 - (1.07)^{-\overline{76\frac{11}{12}}}}{12[(1.07)^{12} - 1]} \right]$$

$$= (5.7647655 - 5.1366077) \times 82176.50031$$

$$= 51619.81$$

$$\text{Interest} = 82176.50031 - 51619.81$$

$$= 30556.69$$

$$\text{Capital Repaid} = 51619.81 - 30556.69$$

$$= 21063.12281$$