

$$4. f(x) = \frac{4x+5}{9-3x}$$

$$a. \lim_{x \rightarrow 1} f(x) = \lim_{x \rightarrow 1} \frac{4x+5}{9-3x} = \frac{1}{12} \quad \text{Continuous}$$

$$c. b. \lim_{x \rightarrow 3} f(x) = \lim_{x \rightarrow 3} \frac{4x+5}{9-3x} = \frac{17}{0} \quad \text{not defined}$$

$$b. \lim_{x \rightarrow 0} f(x) = \lim_{x \rightarrow 0} \frac{4x+5}{9-3x} = \frac{5}{9} \quad \text{Continuous}$$

$$5. \lim_{x \rightarrow \infty} \frac{6e^{4x} - e^{-2x}}{8e^{4x} - e^{2x} + 3e^{-x}}$$

$$\lim_{x \rightarrow \infty} \left( \frac{6e^{4x} - e^{-2x}}{e^{4x}} \right) \left( \frac{e^{4x}}{8e^{4x} - e^{2x} + 3e^{-x}} \right)$$

$$\lim_{x \rightarrow \infty} \frac{(6 - 6e^{-6x})}{8 - e^{-2x} + 3e^{-5x}} = \frac{6}{8} = \frac{3}{4}$$

$$6. \lim_{y \rightarrow 6} g(y) = \lim_{y \rightarrow 6} (1-3y) = -17$$

L.H.L

$$\lim_{y \rightarrow 2} g(y) = \lim_{y \rightarrow 2} (y^2 + 5)$$

$$= 9$$

R.H.L

$$\lim_{y \rightarrow 2^-} g(y) = \lim_{y \rightarrow 2^-} (1-3y)$$

$$= 7$$

## Calculus Assignment 1

$$1. \lim_{h \rightarrow 0} \frac{2(-3+h)^2 - 18}{h}$$

$$\lim_{h \rightarrow 0} \frac{18 - 12h + 2h^2 - 18}{h}$$

$$\lim_{h \rightarrow 0} \frac{h(2h-12)}{h} = 2h-12 = -12$$

$$2. g(x) = \begin{cases} 2x & x < 6 \\ x-1 & x \geq 6 \end{cases}$$

L.H.L

$$\lim_{x \rightarrow 4^-} g(x)$$

$$\lim_{x \rightarrow 4^-} (2x) = 8$$

R.H.L

$$\lim_{x \rightarrow 4^+} g(x)$$

$$\lim_{x \rightarrow 4^+} (2x) = 8$$

$\therefore$  Function is continuous at  $x=4$

b. L.H.L

$$\lim_{x \rightarrow 6^-} g(x)$$

$$= \lim_{x \rightarrow 6^-} (2x) = 12$$

$$\lim_{x \rightarrow 6^+} g(x)$$

$$= \lim_{x \rightarrow 6^+} (x-1) = 5$$

$\therefore$  Function is not continuous

$$3. \lim_{x \rightarrow 9} \frac{x-9}{3-\sqrt{x}} \Rightarrow \lim_{x \rightarrow 9} \frac{(\sqrt{x})^2 - 3^2}{(3-\sqrt{x})(3+\sqrt{x})}$$

$$= \lim_{x \rightarrow 9} \frac{(\sqrt{x}-3)(\sqrt{x}+3)}{(3-\sqrt{x})(3+\sqrt{x})}$$

$$= \frac{-\sqrt{9}+3}{-6}$$

$$= -6$$

$$b. Q(u) = \frac{2}{(6 + (2u) - u^2)^4} = y$$

$$\frac{dy}{du} = \frac{2}{(6 + 2u - u^2)^5} (2 - 2u)$$

$$= \frac{-16(1-u)}{(6 + 2u - u^2)^5}$$

$$\frac{d^2 y}{du^2} = -16 \left[ \frac{(6 + 2u - u^2)^5 (-1) (6 + 2u - u^2)^4}{(6 + 2u - u^2)^{10}} \right]$$

$$= -16 \left[ \frac{(u^2 - 2u - 6) - 2(1-u)^2}{(6 + 2u - u^2)^6} \right]$$

$$= \frac{(2(1-u)^2 - (u^2) + 2u - 6)16}{(6 + 2u - u^2)^6}$$

$$c. P(t) = \ln(1 + t^2)$$

$$P'(t) = \frac{1}{1 + t^2} (2t)$$

$$P''(t) = \frac{(1 + t^2)(2) - 2(t)(2t)}{(1 + t^2)^2}$$

$$= \frac{2 + 2t^2 - 4t^2}{(1 + t^2)^2} = \frac{2 - 2t^2}{(1 + t^2)^2}$$

$$13. P(x) = 2x^3 - 3x^2 - 9x + 12$$

$$P'(x) = 6x^2 - 6x - 9$$

$$P''(x) = 12x - 6$$

$$P''(1) = 12 - 6 = 6$$

$$P'(3) = 18 - 9 = 9$$

$$P''(3) = 36 - 6 = 30$$



8.  $R(\omega) = \frac{3\omega + \omega^4}{2\omega^2 + 1}$

$\frac{d(R(\omega))}{d(\omega)} = \frac{(2\omega^2 + 1)(3 + 3\omega^3) - (3\omega + \omega^4)(4\omega)}{(2\omega^2 + 1)^2}$

9.  $f(x) = 2e^{2x} \cdot 8^x$   
 $f'(x) = 2e^{2x} \cdot 8^x \log 8$

10.  $y = 2^5 - e^2 \ln(2)$   
 $\frac{dy}{dz} = 5 \cdot 2^4 - \left( e^2 \frac{1}{2} + e^2 \ln(2) \right)$   
 $= 5 \cdot 2^4 - \frac{e^2}{2} - e^2 \ln(2)$

10.

11.

a.  $f(x) = (6x^2 + 7x)^4$   
 $= 4(6x^2 + 7x)^3 (12x + 7)$

b.  $f(t) = 5 + e^{4t+7}$   
 $f'(t) = e^{4t+7} (4 + 7 + 6)$

12.

a.  $z = \ln(7 - x^3)$   
 $\frac{dz}{dx} = \frac{1}{7 - x^3} (-3x^2)$

$\frac{d^2 z}{dx^2} = - \left[ \frac{(7 - x^3)(6x)}{(7 - x^3)^2} - \frac{(3x^2)(-3x^2)}{(7 - x^3)^2} \right]$

b.

$$14. f(x) = 4x^3 - 18x^2 + 24x - 7$$

$$f'(x) = 12x^2 - 36x + 24 = x^3 - 3$$

$$f''(x) = 24x - 36$$

$$f''(2)$$

$$f''(2) = 48 - 36 \quad f''(1) = 24 - 36 = -12$$

$$f(1) = 4 - 18 + 24 - 7 \quad f(2) = 32 - 72 + 48 - 7 = -1$$

$$15. f(x) = x^2(x+3) = x^3 + 3x^2$$

$$f'(x) = 3x^2 + 6x = 0$$

$$x^2 + 2x = 0$$

$$x(x+2) = 0$$

$$f(0) = 0$$

$$f(-2) = -8 + 12 = 4$$

$$f'(-1) = 9$$

$$f(1) = 4$$