

ASSIGNMENT

Ques 1

$$\text{Actual length} = 12.5 \text{ cm} = r_1$$

$$\text{Approx radius taken} = 12.65$$

$$\begin{aligned}\text{Actual area} &= \pi r_1^2 \\ &= \pi (12.5)^2 \\ &= 490.8738521\end{aligned}$$

$$\begin{aligned}\text{wrong Area} &= \pi (r_2)^2 \\ &= \pi (12.65)^2 \\ &= 502.7255104\end{aligned}$$

$$\begin{aligned}1 \text{ Absolute error} &= \text{wrong} - \text{Actual} \\ &= 502.7255104 - 490.8738521 \\ &= 11.85165830\end{aligned}$$

$$2 \text{ Relative error} = \frac{\text{Absolute error}}{\text{Actual area}}$$

$$\begin{aligned}&= \frac{11.85165830}{490.8738521} \\ &= 0.024144\end{aligned}$$

$$\begin{aligned}3 \text{ Percentage error} &= \text{Relative error} \times 100 \\ &= 2.4144 \%\end{aligned}$$

Ques 2 $\Rightarrow$

USING INTERPOLATION

$$(i) \quad \begin{array}{ll} X=4 & \longrightarrow 0.60206 \\ X=6 & \longrightarrow 0.7781513 \end{array} \quad \Rightarrow$$

$$\begin{array}{ll} 2 & \longrightarrow 0.1760913 \\ 1 & \longrightarrow \underline{0.1760913} \\ & 2 \end{array}$$

$$5 \longrightarrow \frac{5}{2} \times 0.1760913$$

$$X = 5 \Rightarrow 0.44022825$$

(ii)

$$\begin{array}{ll} X = 4.5 & \longrightarrow 0.6532125 \\ X = 5.5 & \longrightarrow 0.7403627 \end{array}$$

$$\begin{array}{ll} 1 & \longrightarrow 0.0871502 \\ 5 & \longrightarrow 0.435751 \end{array}$$

$X = 5 \longrightarrow 0.435751$

Ques 5-2

$$\begin{array}{r} x \\ 1.5 \\ 2 \end{array} \quad \begin{array}{r} y \\ -6.4375 \\ 4 \end{array}$$

$$= 1.75$$

4

$$y_2 = 0.486191$$

$$y_3 = -1.0202$$

$$y_3 = -0.28773$$

$$y_5 = 0.0933$$

$$u_5 \text{ for } u_{\text{min}} = 1.859375$$

Ques 4

$$f(x) = x^3 - x - 1$$

x	y	
0	-1	-ve
2	$8 - 2 - 1 = 5$	+ve

Formula

$$x_{\text{new}} = x_{\text{old}} - \frac{f(x_{\text{old}})}{f'(x_{\text{old}})}$$

$$f(x) = x^3 - x - 1$$

$$f'(x) = 3x^2 - 1$$

$$\text{Let } x = 0$$

$$f(0) = -1$$

$$f'(0) = -1$$

$$x_1 = 0 - \left[\frac{-1}{-1} \right]$$

$$x_1 = -1$$

$$\begin{aligned} f(x_1) &= -1 - (-1) - 1 \\ &= -1 + 1 - 1 = -1 \end{aligned}$$

$$f'(x_1) = 3 - 1 = 2$$

$$x_2 = -1 - \left[\frac{-1}{2} \right]$$

$$= -1 + \frac{1}{2} = -1 + 0.5 = -0.5$$

$$x_2 = -0.5$$

$$f(x_2) = -0.625$$

$$f'(x_2) = -0.25$$

$$u_3 = -0.5 - \left[\frac{10.625}{10.25} \right]$$

$$= -0.5 - [2.5]$$

$$u_3 = -3$$

$$u_4 = -3 + \left[\frac{-25}{26} \right]$$

$$= -3 + \left[-0.961538 \right] = -2.038461538$$

$$f(u_4) = -7.432009558$$

$$f'(u_4) = 11.46597633$$

$$u_5 = -2.038461538 + \frac{7.432009558}{11.46597633}$$

$$u_5 = -1.390282145$$

$$f(u_5) = -2.296972584$$

$$f'(u_5) = 4.798653328$$

$$u_6 = -1.390282145 + \left(\frac{f(u_5)}{f'(u_5)} \right)$$

$$u_6 = -0.9116118958$$

$$f(u_6) = -0.8459706343$$

$$f'(u_6) = 1.493108746$$

$$u_7 = -0.345028$$

$$f(u_7) = 0.00066456$$

Ques 5

$$A^2 = A$$

$$(a+b)^3 = a^3 + b^3 + 3ab(a+b)$$

$$7A - (I+A)^3$$

$$7A - [I + A^3 + 3A(I+A)]$$

$$7A - [I + A^2A + 3A + 3A^2]$$

$$7A - [I + A + 3A + 3A]$$

$$7A - 7A - I = -I$$

Ques 6 →

$$A = \begin{bmatrix} 1 & -1 & 2 \\ 4 & 0 & 6 \\ 0 & 1 & -1 \end{bmatrix}$$

$$(-2 = -1)$$

$$-1$$

$$|A| = 1(-0-6) + 1(-4) + 2(4)$$

$$= -6 - 4 + 8$$

$$= -2$$

6-8

$$|A| = 1(-6) + 1(-4) + 2(4)$$

$$= -6 - 4 + 8$$

$$= -2$$

-2

-4

$$(\text{adj } |A|) = \begin{bmatrix} -6 & 4 & +4 \\ 1 & -1 & -1 \\ -6 & 2 & -4 \end{bmatrix}$$

$$(\text{adj } A)^T = \begin{bmatrix} -6 & 1 & -6 \\ 4 & -1 & 2 \\ 4 & -1 & -4 \end{bmatrix}$$

$$A^{-1} = \frac{(\text{adj } A)^T}{|A|} = -\frac{1}{2} \begin{bmatrix} -6 & 1 & -6 \\ 4 & -1 & 2 \\ 4 & -1 & -4 \end{bmatrix}$$

Date

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Ques 7

$$\vec{a} = 8\hat{i} - 9\hat{j} \quad \vec{b} = 7\hat{i} - 9\hat{j}$$

$$\vec{a} \cdot \vec{b} = (8\hat{i} - 9\hat{j}) \cdot (7\hat{i} - 9\hat{j})$$

$$= 56 + 81$$

$$= 137$$

$$\begin{array}{r} 56 \\ 81 \\ \hline 137 \end{array}$$

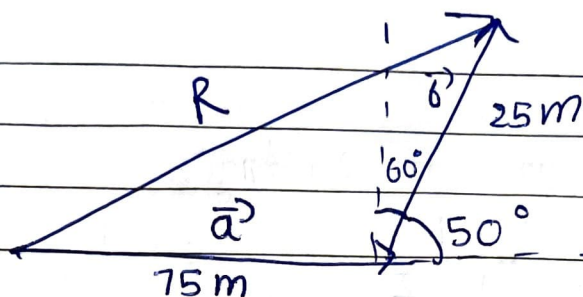
$$\vec{a} \cdot \vec{b} = |\vec{a}| |\vec{b}| \cos \theta$$

$$137 = \sqrt{64+81} \sqrt{49+81} \cos \theta$$

$$0.9978491458 = \cos \theta$$

$$\boxed{3.758556^\circ = \theta}$$

Ques 8 $\Rightarrow$



Date

Displacement vector = $\vec{R}$

$$\vec{R} = \vec{a} + \vec{b}$$

$$R^2 = A^2 + B^2 + 2AB \cos \theta$$

$$\theta = 30^\circ$$

$$R^2 = 75^2 + 25^2 + 2(75)(25) \cos 30^\circ$$

$$R^2 = 9497.595264$$

$$R = 97.4556 \text{ metres}$$

Thus displacement = 97.4556 metres

Ques 9 $\Rightarrow$

Common difference, $d=3$

AP = 101, 104, 107, ..., 998

$$a=101$$

$$a_n = a + (n-1)d$$

$$998 = 101 + (n-1)3$$

$$\boxed{300 = n}$$

$$S_n = \frac{n}{2} (a + a_n)$$

$$= 150 (101 + 998) = 1,64,850$$

Ques 10 $\Rightarrow$

$$96 = 32$$

$$ax^5 = 32$$

$$a_8 = 128$$

$$ax^7 = 128$$

$$\frac{ax^7}{ax^5} = \frac{128}{32}$$

$$x = 2 \text{ or } -2$$

$\hookrightarrow$ rejected as given negative values.

Ques 11

$$(3x+4)^5$$

Using Pascal triangle

$$\begin{array}{ccccccc} & & & & & & 1 \\ & & & & & 1 & 2 \\ & & & 1 & 2 & 1 & \\ & & 1 & 3 & 3 & 1 & \\ & 1 & 4 & 6 & 4 & 1 & \\ 1 & 5 & 10 & 10 & 5 & 1 & \end{array}$$

$$(3x+4)^5 = (3x)^5 + (5 \times 4 \times (3x)^4) + (10 \times (3x)^3 \times 4^2) + (10 \times (3x^2) \times 4^3) + (5 \times 3x \times 4^4) + 4^5$$

$$= 243x^5 + 1620x^4 + 4320x^3 + 5760x^2 + 3840x + 1024$$

Ques 12 =

$$A = \begin{bmatrix} 2 & -3 & 0 \\ 2 & -5 & 0 \\ 0 & 0 & 3 \end{bmatrix}$$

$$A - \lambda I = \begin{bmatrix} 2 & -3 & 0 \\ 2 & -5 & 0 \\ 0 & 0 & 3 \end{bmatrix} - \begin{bmatrix} \lambda & 0 & 0 \\ 0 & \lambda & 0 \\ 0 & 0 & \lambda \end{bmatrix}$$

$$A - \lambda I = \begin{bmatrix} 2-\lambda & -3 & 0 \\ 2 & -5-\lambda & 0 \\ 0 & 0 & 3-\lambda \end{bmatrix}$$

$$\begin{aligned} |A - \lambda I| &= (3-\lambda) [(2-\lambda)(-5-\lambda) + 6] \\ &= (3-\lambda) [-10 - 2\lambda + 5\lambda + \lambda^2 + 6] \\ &= (3-\lambda) (\lambda^2 + 3\lambda - 4) \\ &= 3\lambda^2 + 9\lambda - 12 - \lambda^3 - 3\lambda^2 + 4\lambda \\ &= -\lambda^3 + 13\lambda - 12 \end{aligned}$$

By using hit and trial method
1 is the root of equation

$$\begin{array}{c|cccc} 1 & 1 & 0 & -13 & 12 \\ & 1 & 1 & 1 & -12 \\ \hline & 1 & 1 & -12 & 0 \end{array}$$

$$\lambda^2 + \lambda - 12 = 0$$

$$\lambda^2 + 4\lambda - 3\lambda - 12 = 0$$

$$\lambda(\lambda + 4) - 3(\lambda + 4) = 0$$

$$(\lambda - 3)(\lambda + 4)$$

$$\lambda = 3, -4$$

Eigen values = -4, 1 and 3

Ques 13

$$f(x) = x^3 - 7x^2 + 8x - 3$$

$$f'(x) = 3x^2 - 14x + 8$$

$$x_0 = 5$$

$$f(5) = -13$$

$$f'(5) = 13$$

$$x_1 = x_0 - \frac{f(x_0)}{f'(x_0)} = 5 - \left(\frac{-13}{13}\right) = 6$$

$$f(x_1) = 9$$

$$f'(x_1) = 32$$

$$x_2 = x_1 - \frac{f(x_1)}{f'(x_1)} = 6 - \frac{9}{32} = 5.71875$$

$$f'(x_2) = 0.84787$$

Ques 14

$$(x^2 - x + 1)^4 = ((x-1)^2 + x)^4$$

Using Pascal's triangle

$$\begin{array}{ccccccc}
 & & & & 1 & & \\
 & & & 1 & & 1 & \\
 & & 1 & & 2 & & 1 \\
 & 1 & & 3 & & 3 & & 1 \\
 1 & & 4 & & 6 & & 4 & & 1
 \end{array}$$

$$[(x-1)^2 + x]^4 = (x-1)^8 + 4(x-1)^6x + 6(x-1)^4x^2 + 4(x-1)^2x^3 + x^4$$

Ques 15

$$e^{-x} = 3 \log(x)$$

$$3 \log(x) + e^{-x} - 0$$

x	y
0.6	-0.11673
0.7	0.03188

$$x_0 = 0.6, \quad y_0 = -0.11673$$

$$x_1 = 0.7, \quad y_1 = 0.03188$$

$$1 \quad x_2 = \frac{x_0 + x_1}{2} = 0.65$$

$$y_2 = -0.03921$$

$$2 \quad x_3 = \frac{x_2 + x_1}{2} = 0.675$$

$$y_3 = -0.00293$$

$$3 \quad x_4 = \frac{x_3 + x_1}{2} = 0.6875$$

$$y_4 = 0.01465$$

$$4 \quad x_5 = \frac{x_4 + x_5}{2} = 0.68125$$

$$y_5 = \underline{0.0059}$$