

HOMEWORK.

$$1) \lim_{h \rightarrow 0} \frac{2(-3+h)^2 - 18}{h}$$

$$\Rightarrow \frac{2(9 + h^2 - 6h) - 18}{h}$$

$$\Rightarrow \frac{18 + 2h^2 - 12h - 18}{h}$$

$$\Rightarrow \frac{2h(h-6)}{h}$$

$$\Rightarrow \lim_{h \rightarrow 0} 2h - 12$$

$$\Rightarrow \underline{\underline{-12}}$$

$$2) a) x = 4$$

$$b) x = 6$$

$$g(x) = \begin{cases} 2x & x < 6 \\ x-1 & x \geq 6 \end{cases}$$

$$a) x-1 \rightarrow 4-1 \Rightarrow 3 \quad x$$

$$a) x = 4$$

* continuous, all polynomials are continuous *

Can be only discont. when its def is changing

$$b) x = 6$$

$$LHL = 2 \times 6$$

$$= 12$$

$$RHL = 6-1$$

$$= 5$$

$\therefore$ discontinuous

$$3) \lim_{x \rightarrow 9} \frac{x-9}{3-\sqrt{x}}$$

$$\lim_{x \rightarrow 9} \frac{(\sqrt{x})^2 - 3^2}{3\sqrt{x} - \sqrt{x}}$$

$$\lim_{x \rightarrow 9} \frac{(\sqrt{x}-3)(\sqrt{x}+3)}{(3-\sqrt{x})}$$

$$\lim_{x \rightarrow 9} = \frac{(3-\sqrt{9})(\sqrt{9}+3)}{(3-\sqrt{x})}$$

$$\lim_{x \rightarrow 9} (-\sqrt{x}-3)$$

$$\lim_{x \rightarrow 9} (-\sqrt{9}-3)$$

$$\begin{aligned} \lim_{x \rightarrow 9} &\Rightarrow -3-3 \\ &\Rightarrow -6 \end{aligned}$$

$$4) a) x = -1$$

$$b) x = 0$$

$$c) x = 3$$

$$f(x) = \frac{4x+5}{9-3x}$$

$$a) x = -1$$

$$\frac{-4+5}{9-3(-1)} \Rightarrow \frac{1}{12} \Rightarrow \underline{\underline{\text{continuous}}}$$

$$b) x = 0$$

$$\frac{4(0)+5}{9-3(0)} = \frac{5}{9} \Rightarrow \underline{\underline{\text{continuous}}}$$

$$c) x = 3$$

$$\frac{4(3)+5}{9-3(3)} = \frac{12+5}{0} \Rightarrow \underline{\underline{\text{discontinuous}}}$$

$$5) \lim_{x \rightarrow \infty} \frac{6e^{4x} - e^{-2x}}{8e^{4x} - e^{2x} + 3e^{-x}}$$

$$\lim_{x \rightarrow \infty} \frac{e^{-2x}(6e^{6x} - 1)}{e^{-2x}(8e^{6x} - e^{4x} + 3e^{0x})}$$

$$\Rightarrow \lim_{x \rightarrow \infty} \frac{6 \frac{e^{4x}}{e^{4x}} - \frac{e^{-2x}}{e^{4x}}}{8 \frac{e^{4x}}{e^{4x}} - \frac{e^{2x}}{e^{4x}} + \frac{3e^{-x}}{e^{4x}}}$$

$$\Rightarrow \lim_{x \rightarrow \infty} \frac{6 - 1}{(e^x) \left(8 - \frac{1}{e^{2x}} + \frac{3}{e^{5x}} \right)} = \frac{1 \times (6 - 1)}{\infty}$$

$$6) g(y) = \begin{cases} y^2 + 5 & \text{if } y < -2 \\ 1 - 3y & \text{if } y \geq -2 \end{cases}$$

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$$\Rightarrow \lim_{x \rightarrow \infty} \frac{(6 - 1/e^{6x})}{\left(8 - \frac{1}{e^{2x}} + \frac{3}{e^{5x}} \right)}$$

$$\Rightarrow \frac{1}{\infty} = 0 \quad \frac{6 - 0}{8 - 0 + 3(0)}$$

$$\Rightarrow \frac{3/6}{4/8} = \frac{3}{4} \text{ ans}$$

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$\Rightarrow \frac{1}{\infty} = 0$ $\frac{6 - 0}{8 - 0 + 3(0)}$

$\Rightarrow \frac{36}{48} = \frac{3}{4}$ ans

$$6) \quad g(y) = \begin{cases} y^2 + 5 & \text{if } y < -2 \\ 1 - 3y & \text{if } y > -2 \end{cases}$$

$$a) \quad \lim_{y \rightarrow 6} g(y)$$

$$\Rightarrow \lim_{y \rightarrow 6} 1 - 3y$$

$$\Rightarrow 1 - 3(6)$$

$$\Rightarrow \underline{\underline{-17}}$$

$$b) \quad \lim_{y \rightarrow -2} g(y)$$

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$$\lim_{y \rightarrow -2} g(y)$$

$$\text{LHL} \Rightarrow y^2 + 5$$

$$\Rightarrow (-2)^2 + 5$$

$$\Rightarrow 4 + 5$$

$$\Rightarrow 9$$

$$=$$

$$\text{RHL} \Rightarrow 1 - 3y$$

$$1 - 3(-2)$$

$$1 + 6$$

$$\underline{\underline{7}}$$

$$7) \quad f(t) = (4t^2 - t)(t^3 - 8t^2 + 12)$$

$$\Rightarrow \frac{d}{dt} f(t)$$

$$\Rightarrow (4t^2 - t)(3t^2 - 16t) + (t^3 - 8t^2 + 12)(8t - 1)$$

$$\Rightarrow 12t^4 - 64t^3 - 3t^3 + 16t^2 + 8t^4 - t^3 - 64t^3 - 12 + 96t - 12$$

$$\Rightarrow 20t^4 - 132t^3 + 16t^2 + 96t - 12$$

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$$=$$

$$7) f(t) = (4t^2 - t)(t^3 - 8t^2 + 12)$$

$$\Rightarrow \cancel{4t^4 - 32t^4}$$

$$\Rightarrow \cancel{4t^6}$$

$$\Rightarrow 4t^5 - 32t^4 + 48t^2 - t^4 + 8t^3 - 12t$$

$$\Rightarrow 20t^4 - 128t^3 + 96t - 4t^3 + 24t^2 - 12$$

$$\Rightarrow 20t^4 - 132t^3 + 24t^2 + 96t - 12$$

$$8) R(w) = \frac{3w + w^4}{2w^2 + 1}$$

$$\Rightarrow \frac{3w + w^4 (4w) - (2w^2 + 1)(3 + 4w^3)}{(2w^2 + 1)^2}$$

$$\Rightarrow \frac{\cancel{3w} + 4w^5 - \cancel{2w^2} - 1}{\cancel{3w} + w^4}$$

$$\Rightarrow 3w + 4w^5 - (6w^2 + 8w^5 + 3 + 4w^3)$$

$$\Rightarrow 3w + 4w^5 - 6w^2 - 8w^5 - 3 - 4w^3$$

$$\Rightarrow -4w^5 - 4w^3 - 6w^2 + 3w - 3 //$$

$$9) f(x) = 2e^x - \cancel{8} 8^x$$

$$2e^x - 8^x \log 8 //$$

$$10) \quad y = z^5 - e^z \ln(z)$$

$$\frac{dy}{dz} = \cancel{5z^4 \log z} - \cancel{5z^4} - e^z \ln dz$$

$$5z^4 - \left(\frac{e^z}{z} + \ln(z) \times e^z \right)$$

$$\frac{dy}{dz} = 5z^4 - \frac{e^z}{z} + \ln(z)e^z$$

$$\frac{dy}{dz} = 5z^4 - \frac{e^z}{z} + \ln(z)e^z$$

$$11) a) f(x) = (6x^2 + 7x)^4$$

$$\Rightarrow 4(6x^2 + 7x)(12x + 7)$$

$$\Rightarrow 4(72x^3 + 42x^2 + 84x^2 + 49x)$$

$$b) f(t) = 5 + e^{4t+t^7}$$

$$= 0 + e^{(4t+t^7)} (4 + 7t^6)$$

$$= e^{4t+t^7} \times (4 + 7t^6)$$

$$12) \quad z = \ln(7 - x^3)$$

$$\Rightarrow \frac{dz}{dx} \Rightarrow \frac{1}{(7 - x^3)}$$

$$\Rightarrow \frac{dz}{dx} \Rightarrow \frac{-1}{(7 - x^3)^2} (-3x^2)$$

* b) $Q(v) = \frac{2}{(6+2v-v^2)^4}$

~~$= \frac{2}{4}$~~

$\Rightarrow 2(6+2v-v^2)^{-4}$

$\Rightarrow 2(-4)(6+2v-v^2)^{-5}(2-2v)$

$\Rightarrow \frac{-8(2-2v)}{(6+2v-v^2)^5} \Rightarrow \frac{-16(1-v)}{(6+2v-v^2)^5}$

$-16(1-v)(6+2v-v^2)^4(0+2-2v)$

* c) $f(t) = \ln(1+t^2)$

$\Rightarrow \frac{1}{1+t^2} (2t)$

$\Rightarrow \frac{2t}{1+t^2} \Rightarrow \frac{2t(1+2t) - (1+t^2) \cdot 2}{(1+t^2)^2}$

$\Rightarrow \frac{4t^2 - 1 + t^4 + 2t^2 - 4t^2 - 2 - 2t^2}{(1+t^2)^2}$

$\Rightarrow \frac{2t^2 - 2}{(1+t^2)^2}$

13) $x^3 - 3x^2 - 9x + 12$

$3x^2 - 6x - 9 = 0$

$x^2 - 2x - 3 = 0$

$x^2 - 3x + x - 3 = 0$

$x(x-3) + (x-3) = 0$

$(x+1)(x-3) = 0$

$x = -1, x = 3$

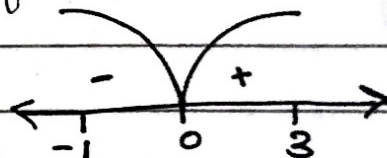
$f'(x) = 6x - 6$

$f'(-1) = -6 - 6 = -12$

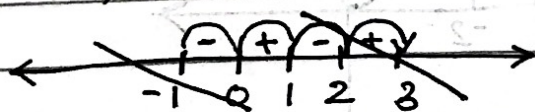
$f'(3) = 18 - 6 = 12$

$f(-1) = -1 - 3 + 9 + 12 = 17$

(max. val)



$f(3) = 27 - 27 - 27 + 12$



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$$4x^3 - 18x^2 + 24x - 7$$

~~$$12x^3 - 36x^2 + 24x - 7 = 0$$~~

~~$$x^3 - 3x^2$$~~

$$12x^2 - 36x + 24 = 0$$

$$x^2 - 3x + 2 = 0$$

$$x^2 - x - 2x + 2 = 0$$

$$x(x-1) - 2(x-1) = 0$$

$$(x-2)(x-1) = 0$$

$$x = 2, x = 1$$

$$f'(x) = 12x^2 - 36x + 24$$

$$f''(x) = 24x - 36$$

$$f''(x) = 48 - 36 = 12$$

$$f''(1) = 24 - 36 = -12$$

$$f(1) = 4 - 18 + 24 - 7 = 3$$

max value

$$f(2) = 32 - 72 + 48 - 7 = 1$$

min val.

$$f(x) = x^2(x+3)$$

$$x^2(x+3) = x^3 + 3x^2$$

$$f'(x) = 3x^2 + 6x = 0$$

$$x^2 + 2x = 0$$

$$x(x+2) = 0$$

$$x = 0, x = -2$$

$$f''(x) = 6x + 6$$

$$f''(0) = 6, f''(-2) = -6$$

At 0, $f(x)$ lies minimum

val & At -2 $f(x)$ has maximum val

$$f(x) = 3x^2 - 6x = 6x - 6 = 6(x-1)$$

$$f'(1) =$$

