

Assignment 2. PRL

1. In practice, the actual profits arising in the future will depend on the actual future experience values of the items.

The insurer will choose a variety of different assumptions in order to determine how quickly the expected future profit changes in varying any particular assumption.

2. Multiple decrement table

x	$q_{x:d}$	$q_{x:w}$	$(aq)_x^d$	$(aq)_x^w$
40	0.000788	0.1	0.000788	0.0999212
41	0.000962	0.05	0.000962	0.0499519
42	0.001124	0.05	0.001124	0.0499448
43	0.001208	0.05	0.001208	0.0499396

$$(aq)_x$$

$$0.8992908$$

$$0.9490861$$

$$0.9489512$$

$$0.9488524$$

$$(aq)_x$$

$$0.8992908$$

$$0.85350439$$

$$0.8099340$$

Unit

t	Pen	$P_{allocated}$	Cost of all	Fund after	Fund before	mgt	Fund after
1	100000	90000	85500	0	90630	453.15	90176.85
2	100000	101500	96425	186601.85	197797.91	988.98	196808.99
3	100000	101500	96425	293233.99	310828.0	1554.14	309274
4	100000	101500	96425	405649	430040.9	2150.204	427891

Ans: A

per unit fund

Yr	Prem - cost all	Expense	Interest	ngt	extra debt	Expected profit
1	10000	12500	-100	453.15	322.94	-2469.79
2	-1500	5000	-260	988.18	291.669	-6067.489
3	-1500	5000	-260	1554.17	210.561	-5416.391
4	-1500	5000	-260	2150.2047	87.107	-4696.90

Q3. (i) The profit vector is the vector end of expected end-year profit for policies which are still in force at the start of each year

(ii) The objective specified for the expected level of profit is termed the 'profit criterion'

It is common for those marketing and selling the products to receive part of their salary in the form of a 'productivity' bonus

Ex:

NPV = 40% of initial sale commission

Profit margin = 3% of FV of premium income

(iii) Profit signature:

$-250, 150, 220, 225$

Let premium = P

2%

$t-1(qp)$

P

2%

1

42

$1.04 P$

20.001104

$(1-0.001104) = 0.998896$

43

$(1.04)^2 P$

20.001208

0.9976893

44

$(1.04)^3 P$

20.001323

0.996365

20.001402

0.9949634

$$\text{EPV Premium} = P + 1.04 P (0.998896) + 1.04^2 P (0.9976893) + (1.04)^3 P (0.9949634)$$

$$\text{EPV of Profit} = \text{EPV of premium} \times 0.05$$

4. The assumption will be the insurer's best estimate of expected future experience. This is term as experience basis.

Assuming that the chosen risk discount rate reflected fully the uncertainty in the assumption, no further margin would be taken.
(pricing basis)

(ii) There may be people surviving. Also considering everyone die, the reserve will be very high.

(ii) Profit vector: $(-20, -35.20, 50, -28.50, -20, 90.21)$

$$4V = \frac{20}{1.06} = 18.86792$$

$$3V = \frac{28.50 + 18.86792(P_{73})}{1.06} \rightarrow 0.965856$$

$$= 44.07895$$

Revised cash flow

$$2V = 50 - 44.07895(P_{72})$$

$$7.275$$

$$1V = \frac{35.20 - 33.2075}{1.06}$$

Revised cash flow = $-20 - P_{(71)}(33.2075)$

$$+ 52.598$$

Revised profit vector:

$$(-52.598, 0, 7.275, 0, 0, 90.21)$$

(i) For a unit-linked life assurance contract, we have:

the unit fund that belongs to the policyholder. This fund keeps track of the premiums allocated to units and benefit payable from this fund to policyholders are denominated in these units. This fund is normally subject to unit fund charges.

the non-unit fund that belongs to the company. This fund keeps track of the premiums paid by the policyholder which are not allocated to units together with units fund charges from the unit fund. Company expenses will be charged to this fund together with any non-unit benefits payable to policyholders.

(ii) It is a principle of prudent financial management that once sold and funded at outset, a product should be self-supporting.

However, some products can give profit signatures which have more than one financing phase. In such cases, reserves are required at earlier durations to eliminate future negative cash flows, so that the office does not expect to have to input further money in the future.

		30	31	32	33
6	Yr	1	2	3	4
		-250	-400	-600	1500

Amq notality Ultimate

x	Yr	q_x	P_x	
30	1	0.000590	0.99941	P_{30}
31	2	0.000602	0.999398	P_{31}
32	3	0.000612	0.999386	P_{32}
33	4	0.000636	0.999364	P_{33}

(i) NPV

$$= \frac{-250}{1.06} - \frac{400}{1.06^2} \times P_{30}^{0.99941} - \frac{600}{1.06^3} \times 2P_{30}^{0.998803} + \frac{1500}{1.06^4} \times 3P_{30}^{0.998192}$$

$$= \frac{-250}{1.06} - 355.7885 - 503.171 + 1185.99$$

91.18 ←

(ii) Zeroisation

$$2N = \frac{+600}{1.03} = 582.524$$

$$1N = \frac{400 + 582.524(P_{31})}{1.03}$$

$$= 1020.91$$

$$\text{Revised cash flow} = -250 - 1020.91 P_{30} = -1270.91$$

Profit vector: $(-1270.316, 0, 0, 1500)$

$$NPV = \frac{-1270.316}{1.08} + 0 + 0 + \frac{1500}{1.08^4} \quad \text{by } P_{30}$$

$$= -75.66$$

NPV after zeroization is smaller

7. 1/

Multiple table

x	$z_{x,d}$	i	$(99)^0$
61	0.006433	0.06	0.059614
62	0.009696	0.06	0.0594182
63	0.01137	0.06	0.0593196
64	0.012716	0.06	0.05923704

(6-1) 99

0.933953	
0.9308858	0.933953
0.9293404	0.8694034
0.92821696	0.8079717

Unit

Yrs	P	Pre all	Cost All	Fund after	Fund kept	mgd	Fund
1	3000	12000	11400	0	11970	179.55	11790.45
2	3000	27000	25650	37440.25	39312.47	589.682	38722.8
3	3000	30000	27000	65722.80	69008.94	1035.13	67973.80
4	3000	33000	27000	94973.805	99722	1495.83	93228.17

Non-unit fund

Yrs	Prem-cost all	Expense	Interest	mgd	Extm death	net unit	Profit
1	18000	11000	245	179.55	567.45	0	6857.1
2	3000	2600	14	589.682	594.143	0	409.544
3	0	2600	-91	1035.13	363.177	0	-2019.047
4	-3000	2600	-196	1495.83	22.556	95716.42	-100034.145

(i) Let P be the annual premium required to meet the company's profit criteria.

(a) Multiple decrement table

Here not all decrements are uniform as whilst deaths can be assumed to be uniformly distributed over the year, surrenders occur only at the year end.

$$(aq)_x^d = q_x^d$$

$$(aq)_x^w = (1 - q_x^d) p_x^w$$

x	q_x^d	q_x^w	$(aq)_x^d$	$(aq)_x^w$	$(ap)_x$	${}_{t-1}(ap)_x$
45	0.001465	0.05	0.001465	0.049927	0.948608	1
46	0.001622	0.05	0.001622	0.049919	0.948459	0.948608
47	0.001802	0.05	0.001802	0.049910	0.948288	0.899716

unit fund

Yrs	P	Pre all	Cost all	Fund after all	Fund before mgt	mgt	Fund at end
1	P	$0.35P$	$0.3325P$	0	$0.349125P$	$0.001745625P$	$0.347379P$
2	P	$1.05P$	$0.9975P$	$1.34487P$	$1.412123P$	$0.007061P$	$1.405062P$
3	P	$1.05P$	$0.9975P$	$2.40256P$	$2.52269P$	$0.012613P$	$2.510077P$

Non-unit fund

Yrs	Prem-cost all	Expense	Interest	mgt	Profit Vector
1	$0.6675P$	$0.2P + 250$	$0.0187P - 10$	$0.001745625P$	$0.487946P - 260$
2	$0.0025P$	$0.025P + 50$	$-0.0009P - 2$	$0.007061P$	$-0.016339P - 52$
3	$0.0025P$	$0.025P + 50$	$-0.0009P - 2$	$0.012613P$	$-0.010787P - 52$

Yr	Profit Vector	Inforce Prob	Discount factor	EPV of profit
1	$0.487946P - 260$	1	0.925926	$0.451801P - 240$
2	$-0.016339P - 52$	0.948608	0.857339	$-0.013298P - 42.290$
3	$-0.010787P - 52$	0.899716	0.793832	$-0.007704P - 37.14$

10.	z_u	P_u	$(1-p)$
50	0.015	0.985	1
51	0.015	0.985	0.985
52	0.015	0.985	0.970225
53	0.015	0.975	0.955671

unit fund

Yr	P	Pulled out	Cost all	Policy fee	Fund after	Fund before	mgf
1	25000	17500	15750	500	0	16317.5	81.5875
2	25000	27500	24750	500	40485.91	43319.92	216.5996
3	25000	27500	24750	500	67353.3	72068.05	360.34
4	25000	27500	24750	500	95957.7	102674.7	513.37

Fund at end
16235.912
43103.32
71707.70
1012161.32

non-unit fund

Yr	Pre-cost all	Expense	Policy fee	Interest	mgf	extra death
1	7500	9250	3500	500	437.5	81.5875
2	250	1100	500	-24.5	216.5996	328.4501
3	250	1100	500	-24.5	360.34	0
4	250	1100	500	-24.5	513.37	0

-374.5

Profit vector

6037.6275
-486.3506
-44.16
138.87

Discount factor not given