

10.  $T = 3$   $n = 1000$

$$H_0: \lambda \leq 3,1000 = T = 3$$

$$H_1: \lambda > 3,100 = T \neq 3$$

~~$$1 - e^{-T} \frac{x}{T}$$~~

11.  ~~$\sum x^2 = 4$~~   
 $E(x) = \frac{2,13,200}{12} = 17,766$

$$V(x) = 102.900736$$

$$\sum x^2 = 4,243,360,000$$

$$E(x) = 17,764$$

an approximate weighted measure for estimating a better

Both of them will be termed consistent if the sample size ~~is~~ goes on increasing still the MSE is small.

(1)  $\theta = E(g(x))$

(2)  $\theta = E(g(x))$  - Bias

\*) t test

$$\frac{\bar{x} - \mu}{s/\sqrt{n}} \sim t_{n-1}$$

mean - 0

variance -  $\frac{k}{k-2}$

~~$$50 \pm t_{n-1} s/\sqrt{n}$$~~

~~$$50 \pm 2.8221 \times \sqrt{48.667/10}$$

$$(50 + 6.223) \quad (50 - 6.223)$$

$$= 56.223 \quad 43.777$$~~

~~$$43.777 < x < 56.223$$~~

~~$$50 \pm \sqrt{\quad}$$~~

$$50 \pm 3.250 \times \sqrt{48.667/10}$$

$$50 \pm 7.16969$$

$$42.831 < x < 57.169$$



The primary condition to check whether the mean ~~is~~ equal is that the sample should be large enough

It is not possible to identify whether the condition is met or not because the population size is unknown

$$35.05 \pm 1.96 \cdot \sqrt{67.875}$$

$$35.05 \pm 17.96$$

$$\cancel{52.96}$$

$$17.09 \times < 53$$

$$2. \hat{\theta} = \theta$$

$$\cancel{E(\hat{\theta}) = \theta}$$

If  $E(g(x)) = \theta$  then it is an unbiased estimator

Bias:

$$E(g(x)) - \theta$$

Mean square error = variance + bias<sup>2</sup>

mean square error is used to measure the efficiency of biased estimators than unbiased ones.

(6)

 $U(0, 5)$ 

$$L = \frac{1}{5^2}$$

m.l.e for uniform  
 $U(0, \theta)$

$$L = \frac{1}{\theta^n}$$

$$\frac{d}{d\theta} \ln L(\theta) = \frac{-n}{\theta}$$

$$= \frac{-n}{\theta}$$

$$6. H_0: p = 0.1$$

$$H_1: p > 0.1$$

7. Public mean = 30  
Private mean = 35.05

$$\text{variance} = \frac{16268806 - 8614 \cdot 8100}{8}$$

$$= 64.25$$

$$\frac{10669 - 11599 \cdot 11056}{8}$$

$$= 67875$$

The point  
whether  
that the  
large

It is not  
the con  
because  
unkno

35.05

35.05

52.9  
17.0

2.  $\hat{\theta} = \theta$   
 $\hat{\theta} = \theta$   
 $\hat{\theta} = \theta$   
estimator

Bias  
 $E(g)$

mean

mean  
mean  
biased  
ones.



$$2\bar{x} - s\sqrt{12} = 2a$$

~~$$2\bar{x} - s\sqrt{12} = a$$~~

$$\bar{x} - \frac{s\sqrt{12}}{2} = a$$

$$\frac{a+b}{2} = \bar{x}$$

$$\frac{(b-a)^2}{12} = s^2$$

$$a+b = 2\bar{x}$$

$$a = 2\bar{x} - b$$

$$\frac{(b-a)}{\sqrt{12}} = s$$

~~$$b - 2\bar{x} + b =$$~~
~~$$2\bar{x} = s^2$$~~

$$b - a = s\sqrt{12}$$

$$b = s\sqrt{12} + a$$

~~$$a + b = 2\bar{x}$$~~

~~$$a + s\sqrt{12} = a$$~~

~~$$2a + s\sqrt{12} = 2\bar{x}$$~~

~~$$2a = \frac{2\bar{x} - s\sqrt{12}}{2}$$~~

$$a = b - s\sqrt{12}$$

$$a + b = 2\bar{x}$$

$$b - s\sqrt{12} + b = 2\bar{x}$$

$$2b = 2\bar{x} + s\sqrt{12}$$

$$b = \frac{2\bar{x} + s\sqrt{12}}{2}$$

$$\frac{(G_i - E_i)^2}{E_i}$$

$$69.44, 42.25, 11.11, 32.11.1, 34.02$$

$$4. f(x) = \frac{C\beta}{(\alpha + \beta)^4}$$

$$\int \alpha \cdot \frac{C\beta}{(\alpha + \beta)^4}$$

$$\int \frac{\alpha C\beta}{(\alpha + \beta)^4}$$

$$S. \frac{a+b}{2} = \bar{x} \quad \frac{(b-a)^2}{12} = s^2$$

$$2\bar{x} - a - b$$

$$(b^2 - 2ab + a^2)$$

$$\frac{(2\bar{x} - a)^2 - 2a(2\bar{x} - a) + a^2}{12}$$

$$4\bar{x}^2 -$$

$$\frac{(b-a)^2}{12} = s^2$$

$$\frac{2\bar{x} - a - b}{\sqrt{12}} = s$$

$$2\bar{x} - 2a = s\sqrt{12}$$



3.  $n C_x \cdot p^x \cdot q^{n-x}$

$L = \prod$

$$\begin{aligned} & 4 C_0 p^0 q^{4-0} \cdot 4 C_1 p^1 q^{4-1} \cdot 4 C_2 p^2 q^{4-2} \cdot 4 C_3 p^3 q^{4-3} \cdot 4 C_4 p^4 q^{4-4} \\ & 4 C_0 p^0 q^4 \cdot 4 C_1 p^1 q^3 \cdot 4 C_2 p^2 q^2 \cdot 4 C_3 p^3 q^1 \cdot 4 C_4 p^4 q^0 \end{aligned}$$

$$q^4 \cdot 4 p q^3 \cdot 6 p^2 q^2 \cdot 4 p^3 q \cdot p^4 q^0$$

$$= (1-p)^4 \cdot 4 p (1-p)^3 \cdot 6 p^2 (1-p)^2 \cdot 4 p^3 (1-p) \cdot p^4 q^0$$

$96 \cdot p^1 (1-p)^1$

Taking  
Log L =  $10 \log p + 10 \log (1-p)$   
Taking

$$= \frac{10}{p} + \frac{10}{(1-p)} + C$$

$$\frac{10(1-p) + 10p}{p(1-p)}$$

|    |    |    |   |   |
|----|----|----|---|---|
| 0  | 1  | 2  | 3 | 4 |
| 86 | 75 | 16 | 2 | 1 |

| x | $O_i$ | $C_i$ |
|---|-------|-------|
| 0 | 86    | 36    |
| 1 | 75    | 36    |
| 2 | 16    | 36    |
| 3 | 2     | 36    |
| 4 | 1     | 36    |

(2)

$$\left( \frac{1}{n-1} \left( \sum \sigma^2 + u^2 \right) - n \left( \frac{\sigma^2}{n} + u^2 \right) \right)$$

$$\frac{1}{n-1} (n\sigma^2 + nu^2 - \sigma^2 - nu^2)$$

$$\frac{1}{n-1} (n-1) \sigma^2$$

$$E(S^2) = \sigma^2$$

$$\text{var} \left( \frac{n-1}{\sigma^2} S^2 \right) = n-1$$

$$= (2n-1)$$

$$\frac{S^2}{\sigma^2} = \frac{\sigma^2}{n-1} (n-1) \cdot \sigma^2$$

$$\text{var} \left( \frac{n-1}{\sigma^2} S^2 \right) = 2n-1$$

$$\Rightarrow \text{var}(S^2) = \frac{\sigma^4}{n-1} \times 2n-1$$

$$= \frac{2\sigma^4}{n-1}$$

~~2~~+

④ Probability is 0.000 according to formulae table



q is 0.140, 0.226

① Tags assignment  $n+1$   
 $\bar{x} \pm z_{\alpha/2} \sigma \sqrt{n}$

$$\bar{x} \pm 1.96 \times \frac{200}{200} / 200$$

$$2. \sum x_i = 104$$

$$\sum \sigma^2 = 102 \sigma^2$$

$$\bar{x} = \frac{104}{n}$$

$$\sigma^2 = \frac{102 \sigma^2}{n^2}$$

$$\bar{x} = 4$$

$$\sigma^2 = \frac{\sigma^2}{n}$$

$$E(\sigma^2) = \sigma^2$$

using method of moments  
 $E(\sigma^2) = \frac{1}{n-1} \sum (x_i - \bar{x})^2$

$$\frac{1}{n-1} (102 - 4^2)$$