

$$Q1) \text{ forward rate} = \frac{0.06 \times 0.15 - 0.05 \times 0.5}{0.25}$$

$$= 0.8$$

$$= 8\%$$

Since the FRA rate is 7%, profit can be made by borrowing at 5% for 6 months, then borrowing between 6th and 9th month at 7% by entering into FRA & then lending for 3 months at 6%.

Q2) a) Here, a forward contract could give better outcome compared to a future contract because the company will make losses by hedging. If the company hedges using forward contract, the entire loss will be realized at end whereas, in future contract the company can realise its loss day by day which is not very preferable based on present value.

b) Here, a future contract would give better outcome compared to a forward contract because the company will make profit by hedging. If the company hedges using forward contract, the profit will be released at end, which is not very preferable whereas, in future contract, the company will realise its profit day by day which is preferable on the basis of present value.

c) Here the future contract would have better outcome compared to forward contract because future contract would have positive cash flows initially & the negative cashflows later.

d) Here the forward contract would have better outcome compared to future contract because forward contract would have negative cash flow initially & the positive cashflow later.

- Q3) The company might want to choose the delivery date least favourable to the bank. The bank might price the product based on this assumption.

If the domestic interest rate is higher than foreign exchange rate then:-

- 1) The latest delivery date will be assumed when the company has long position.
- 2) The earliest delivery date will be assumed when the company has short position.

If the domestic interest rate is lower than foreign exchange rate then:-

- 1) The latest delivery date will be assumed when the company has short position.
- 2) The earliest delivery date will be assumed when the company has long position.

The bank will make profits if the company chooses a delivery date ~~which is~~ ~~sub~~

$$\begin{aligned} \text{Q4) Contract value} &= 10,000 [100 - 0.25(100 - 92)] \\ &= 10,000 [100 - 0.25(100 - 92)] \\ &= 980,000 \end{aligned}$$

Number of contracts (N) =

$$\frac{\text{Portfolio forward value}}{\text{Future contract price}} \times \frac{\text{Portfolio duration}}{\text{Futures duration}}$$

$$\frac{\text{Portfolio duration}}{\text{Futures duration}} = 2 \left[\because \text{commercial paper matures in } 50 \text{ days} \right]$$

twice that of future

$$\begin{aligned}
 \therefore N &= \frac{\text{Portfolio forward value}}{\text{Future contract price}} \times 2 \\
 &= \frac{48,20,000}{980,000} \times 2 \\
 &= 9.84
 \end{aligned}$$

$\therefore$ Therefore 10 contract should be shorted.

(35) No. of short future contracts required :-

$$\begin{aligned}
 &\frac{\text{Portfolio forward price}}{\text{Future contract price}} \times \frac{\text{Portfolio duration}}{\text{Future duration}} \\
 &= \frac{100,000,000}{123,000} \times \frac{4}{9} \\
 &= 364.3
 \end{aligned}$$

$\therefore$ 364 short contract are required

a) No. of contracts should be shorted to :-

$$\frac{100,000,000 \times 4}{123,000 \times 7} = 468.4$$

$\therefore$ 468 contracts should be shorted.

b) Here, the loss on the bond portfolio will probably be more than the profit on the short future position. It is because the profit depends on the size of movement in long-term rates whereas the loss depends on the size of movement in medium term rates. duration-based hedging assumes that the movement in the two rates are equal.

Q6) X has a comparative advantage in yen market and wants to buy dollars.

Y has a comparative advantage in dollar market and wants to buy yen.

Per annum difference

1.5% $\rightarrow$ yen rates

0.4% $\rightarrow$ dollar rates

$$\text{Total gain from swap} = (1.5 - 0.4)\% \\ = 1.1\% \text{ per annum}$$

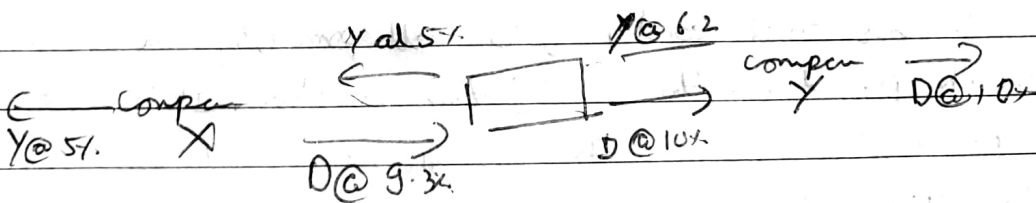
Bank $\rightarrow$ 0.5 per annum

leaving 0.3% for X & Y

X borrows dollars at $\rightarrow 9.6 - 0.3 = 9.3\%$

Y borrows yen at $\rightarrow 6.5 - 0.3 = 6.2\%$

All foreign exchange risk is borne by bank



Y = yen

D = dollar

Q7) The swap rate is the fixed rate that the swap receiver demands in exchange for the uncertainty of having to pay a short-term rate.

At the same time the swap rate for a particular maturity is the swap par yield for the maturity. Here, the par yield is the coupon rate on a fixed income instrument that makes its price equal to the principal at a given maturity.

Q8) The bank can offset the risk by entering into interest rate swaps with other financial institutions in which the bank signs a contract which states to pay fixed rate & receive floating rate.

Q9) Correct discount rate:-

(2). p.a with quarterly compounding

11.8% p.a with continuous compounding

The next floating payment: $0.118 \times 100 \times 0.25$

$$= 2.95$$

- The value of floating rate bond: $102.05e^{-0.1182 \times 4}$

$$= 100.941$$

The value of fixed rate bond:-

$$2.5e^{-0.1182 \times 1/2} + 2.5e^{-0.1182 \times 5/2} + 2.5e^{-0.1182 \times 9/2} +$$

$$2.5e^{-0.1182 \times 13/2} + 102.5e^{-0.1182 \times 14/2}$$

$$= 98.678$$

The value of swap = floating rate - fixed rate

$$= 100.941 - 98.678$$

$$= \$2.263 \text{ million}$$

Q10) Forward rate = 8%.

Strike rate = 7.6%

Time to maturity = 4 years

Risk free rate = 8%

Volatility = 25%

Pay off from swaption = $\max(0.076 - R, 0)$

Value of annuity at the end of 5, 6, 7, 8 & 9 years

$$\sum_{i=5}^9 e^{-0.078i} = 2.972$$

The value of swaption in million dollars =

$$2.914 [0.076 N(-d_2) - 0.08 N(d_1)]$$

$$d_1 = \frac{\ln(0.08 / 0.076) + 0.25^2 \times 2}{0.25 \sqrt{4}} = 0.3526$$

$$d_2 = d_1 - 0.5 \sqrt{4} = -0.1474$$

$$\text{Swaption} = 2.914 [0.076 N(0.3526) - 0.08 N(-0.1474)]$$

$$\approx 0.0401$$

$$\approx \$40,100$$

Q11) $S_0 = \frac{1}{1.48} = 0.6757$

$$R = 1/1.5 = 0.6667$$

$$r = 0.08$$

$$\sigma = 0.12$$

$$q = 0.04$$

$$T = 1$$

$$\text{Value of derivative} = 10,000 N(-d_2) e^{-0.08T}$$

Hence

$$d_2 = \ln(0.6757/0.6667) + (0.08 - 0.04(-0.12)^{1/2})$$

$$= 0.3853$$

$$N(-d_2) = 0.3501$$

$$10,000 \times 0.3501 \times e^{-0.08} = \text{Derivative}$$

$$= \$3231$$

$$\text{In dollars } 3231 \times 1.48 = \$4782$$

Q12) In an Asian option the payoff becomes more certain as the time passes and the delta always approaches zero as the maturity date is approached. This makes delta hedging easy.

Q13) This is a cash-or-nothing call,

Value is $100 N(d_2) e^{-0.08 \times 0.5}$ where

$$d_2 = 0.1826$$

$$\text{value of derivative} = 100 \times 0.4276 \times e^{-0.08 \times 0.5}$$

$$= \$41.08$$