

Assignment 1

Q1 Calculate the mean, median, mode, standard deviation and inter quartile range of the following data.

1) 4, 7, 9, 9, 11, 15, 18, 18, 18, 25

Ascending Order

4, 7, 9, 9, 11, 15, 18, 18, 18, 25

$N=10 \rightarrow$ i.e. Even

$$\text{① Mean} = \frac{4+7+9+9+11+15+18+18+18+25}{10}$$

$$= \frac{134}{10}$$

$$\boxed{\text{Mean} = 13.4}$$

② Median

$N=10 \rightarrow$ i.e. Even

$\therefore$ The median is between middle two no. i.e. 11 and 15

$$\therefore \text{median} = \frac{11+15}{2}$$

$$= \frac{26}{2}$$

$$\boxed{\text{Median} = 13}$$

③ Mode

here mode = 18 as it is repeated 3 times i.e. maximum.

X	$X - \bar{X}$	$(X - \bar{X})^2$
4	-9.4	88.36
7	-6.4	40.96
8	-4.4	19.36
9	-4.4	19.36
11	-2.4	5.76
15	2.4	5.76
18	5.4	29.16
18	5.4	29.16
18	5.4	29.16
25	12.4	153.76
Total = 134		420.8

(X) mean = 13.4

$$\text{var} = \frac{\sum (X - \bar{X})^2}{n}$$

$$= \frac{420.8}{10}$$

$$\text{var} = 42.08$$

$$\text{④} \therefore \text{S.D} = \sqrt{42.08}$$

$$\text{S.D} = 6.48690$$

$$\text{⑤ median} = 13$$

i.e 50% is present Before 13 and
50% after 13.

Q.2 It is assumed that claims arising on an industrial policy can be modelled as a Poisson process at a rate of 0.5 per year

$$\rightarrow i) \lambda = 0.5 \\ x = 0$$

$$P(X=0) = \frac{(0.5)^0 e^{-0.5}}{0!}$$

$$= \frac{1}{e^{0.5}}$$

$$= 0.6065$$

Q4) Given male = 10
Female = 8

out of 10 male = 6 qualified candidates
out of 8 female = 7 qualified candidates

Find - Select team of two workers
consisting qualified people
and least one female.

Solution

Case 1 = Out of two qualified
one man and one female

$$\begin{aligned} P(1) &= {}^nC_r = \\ &= {}^6C_1 \times {}^7C_1 \\ &= 6 \times 7 \end{aligned}$$

$$P(1) = 42 \rightarrow \text{①}$$

Case 2 = Out of two qualified all
two are female

$$\begin{aligned} P(2) &= {}^7C_2 \\ &= \frac{7!}{2!(5!)} = \frac{7 \times 6 \times 5!}{2 \times 1 \times 5!} \end{aligned}$$

$$P(2) = 21$$

$$\begin{aligned}
 P(\text{At least a female}) &= P(1) \text{ or } P(2) \\
 &= P(1) + P(2) \\
 &= 42 + 21 \\
 &= 63
 \end{aligned}$$

Q5- Given

(Level 1) = next day delivery

(Level 2) = 2-day delivery

(Level 3) = 3-day delivery

Let 100 package be delivered

L1 delivery = 40% $\rightarrow$ 40 packages

L2 delivery = 50% $\rightarrow$ 50 packages

L3 delivery = 10% $\rightarrow$ 10 packages

Late L1 delivery = 20% $\rightarrow$ 20 packages

Late L2 delivery = 40% $\rightarrow$ 40 packages

Late L3 delivery = 10% $\rightarrow$ 10 packages

Find $P(\text{Late package via Level 2})$

$$P(\text{LP via L2}) = \frac{40}{50}$$

$$P(\text{LP via L2}) = 0.8$$

$$\begin{aligned} \text{Q11} \rightarrow & \text{Total children} = 7 \\ & \text{Boys} = 5 \\ & \text{Girls} = 2 \end{aligned}$$

$$P(B) = \frac{5}{7} \Rightarrow P(G) = \frac{2}{7}$$

$$P(\text{Next 3 Boys}) = \frac{3 \times 5}{7}$$

$$\begin{aligned} &= 2 \\ P(\text{Next 3 Girls}) &= \frac{3 \times 2}{7} \\ &= 0.428 \end{aligned}$$

$$\begin{aligned} \therefore P(\text{Next 3 boys}) &= 1 - 0.428 \\ &= 0.571, \end{aligned}$$

Q12) $\lambda = 10 \text{ per day}$
 ce) $x = 2$

$$P(X=2) = \frac{(10)^2 e^{-10}}{2!}$$

$$= \frac{100}{2} e^{-10}$$

$$\begin{aligned} &= 50 \times 0.000045 \\ &= 0.00225 \end{aligned}$$