

Dhanini Shah

SRM Assignment 1

Q1)		04		
AY	0	1	2	3
2001	1245	999	610	356
2002	1455	1088	723	
2003	1567	1079		
2004	1491			

Year	Inflation adjustment			
2001	(1.021) (1.072) (0.992)	2	1.02498	
2002	(1.072) (0.992)	2	1.003904	
2003	0.992	2	0.992	
2004	1	2	1	

Incremental mid 2004 priced adjustment

	0	1	2	3
2001	1276.11	1002.9	605.10	356.10
2002	1460.68	1079.3	723	
2003	1554.46	1079		
2004	1491			

Cumulative claims

	0	1	2	3
2001	1276.11	2279.07	2884.13	3240.13
2002	1460.68	2539.98	3262.98	
2003	1554.46	2633.46		
2004	1491			
af	1.7366	1.2756	1.1234	

Developed

	0	1	2	3
2001	1276.11	2279.01	2884.13	3240.13
2002	1460.68	2539.98	3262.98	3665.74
2003	1554.46	2633.46	3357.245	3773.87
2004	1491	2589.36	3302.97	3710.69

Incremental prices

	0	1	2	3
2004	1098.36	712.64		
2004		1098.36	712.64	407.7
Inflation index		1.025	1.050625	1.076591
Adjustment		1125.819	748.72	439.05

Total : $2313.5875 \times 1000 = 2313587.5$

(ii) Ultimate amount for 2004 policies = 5250000×0.73
Bornheutter ferguson method, = 3937500

cds	-	2.48891	1.43304	1.82343
Reverse	1	1.2343	1.43304	2.48071
1/f	1	0.81017	0.69778	0.4018
1-1/f	0	0.18983	0.3022	0.5982

DY	EL
1	$3937.5 (1/1.43304 - 1/2.4887) = 1165.57$
2	$3937.5 (1/1.2343 - 1/1.433) = 757.24$
3	$3937.5 (1 - 1/1.2343) = 432.61$

Adjusting for inflation:

B

~~Q#~~ 1 $1165.51 \times 1.025 = 1194.68$

~~2~~ 2 $757.24 \times 1.0586 = 795.59$

~~3~~ 3 $432.61 \times 1.076391 = 465.87$

Total emerging liability : $1194.68 + 795.59 + 465.87$

$$: 2456.09 \times 1000$$

$$= 2456090 .$$

Q3) Doubt as years are not same

82]

V/W

Incurred

Development year

2005

3512

7210

9563

2006

2889

6723

2007

3876

5

Loss ratio = 87%

Total claims paid = 20103000

Premium Income

2005

11041

2006

11314

2007

12549

10

Ans)

1

2

3

Ultimate

2005

3512

7210

9563

9563

2006

2889

6723

2007

3876

15

M

2.1767

1.3264

1

F

2.8872

1.3264

1

(1 - 1/F)

0.6536

0.24608

0

1

AY

2007

2006

2005

20

EP

12549

11314

11041

JUL

10917.63

9843.18

9605.67

EL

7135.76

8422.21

0

RL

3876

6723

9563

UL

11005.76

9145.21

9563

25

Total UL : 29713.97 X 1000 (as it is in 1000s)

∴ Reserves = 29713.97 - 20103000

= 29713970 - 20103000

= 9610970

30

84) ACPC cumulative

py

	0	1	2
2005	530.63	720.75	830.532
2006	491.32	716.092	
2007	753.84		

Grossing up factors

	0	1	2	Ultimate
2005	63.891%	86.78%	100%	830.532
2006	59.5426%	86.28%		825.1714
2007	61.716%			1221.4591

No. of claims

py

	0	1	2
2005	88	121	156
2006	128	163	
2007	98		

Grossing up factors

	0	1	2	Ultimate
2005	52.56%	77.56%	100%	156
2006	60.96%	77.56%		210.149
2007	56.738%			172.73

Projected ultimate loss

Acc year

2006 $825.1714 \times 210.149 = 173408.9445$

2007 $1221.4591 \times 172.723 = 210975.0042$

2005 + 129562.79

513946.9407

Outstanding claims = $513946.9407 - (73876 + 116723 +$

015 = 193784.9384 129563

Q5)

$$X \sim \text{Exp}(\lambda) \rightarrow 2006$$

$$Y \rightarrow 2007$$

$$(i) \text{ Pf: } Y = kX$$

$$\therefore P(Y < y) = P(kX < y) \\ = P(X < y/k)$$

$$= \int_0^{y/k} \lambda e^{-\lambda z} dz$$

$$\text{where } kz = x$$

$$= \int_0^y \lambda e^{-\frac{\lambda x}{k}} \frac{dx}{k}$$

$$= \int_0^y \frac{\lambda}{k} e^{-\frac{\lambda x}{k}} dx$$

→ pdf of exponential distribution.

$$Y \sim \text{Exp}\left(\frac{\lambda}{k}\right)$$

$$(ii) P(X > M) = e^{-\lambda M}$$

$$P(Y > M) = e^{-\lambda M/k}$$

$$L = C x e^{-4\lambda M} \times \prod (\lambda e^{-\lambda x_i}) x e^{-6\lambda M/k} \times \prod \left(\frac{\lambda}{k} e^{-\lambda y_i/k} \right)$$

$$\log L = C' - 4\lambda M + 10 \log \lambda - \lambda \sum x_i - \frac{6\lambda M}{k} + 12 \log \lambda - \frac{\lambda}{k} \sum y_i$$

$$= C - 4\lambda M + 22 \log \lambda - 13500 \lambda - \frac{6\lambda M}{k} - \frac{17000 \lambda}{k}$$

$$\frac{d \log L}{d \lambda} = -4M + \frac{22}{\lambda} - 13500 - \frac{6M}{k} - \frac{17000}{k}$$

$$-4M + 22 \cdot -15000 - \frac{6M}{K} - \frac{17000}{K} = 0$$

$$\lambda = 22$$

$$\frac{15000 + 17000}{K} + \frac{4M}{K} + \frac{6M}{K}$$

$$(ii) a) \lambda = \frac{22}{\frac{15000 + 17000}{1.1} + \frac{4 \times 1600}{1.1} + \frac{6 \times 1600}{1.1}}$$

$$= 0.000499$$

b) Expected payment

$$\int_0^M \lambda x e^{-\lambda x} dx + M \int_M^{\infty} \lambda e^{-\lambda x} dx = \left[-x e^{-\lambda x} \right]_0^M + \int_0^M e^{-\lambda x} dx + M \left[-e^{-\lambda x} \right]_M^{\infty}$$

$$= -M e^{-\lambda M} + \left[-\frac{1}{\lambda} e^{-\lambda x} \right]_0^M + M e^{-\lambda M}$$

$$= \frac{1}{\lambda} \left[1 - e^{-\lambda M} \right]$$

$$= \frac{1}{0.000499} (1 - e^{-0.000499 \times 1600})$$

$$= 1102.107$$

$$\mu = \frac{\lambda}{1.05 \times 1.1}; \text{ need Retention } R \text{ so}$$

$$1102.107 = \int_0^R x \mu e^{-\mu x} dx + R \int_R^{\infty} \mu e^{-\mu x} dx$$

$$= \frac{1}{\mu} (1 - e^{-\mu R}) = \frac{1.05 \times 1.1}{0.0004999} (1 - e^{-\frac{0.0004999}{1.05 \times 1.1} R})$$

$$0.47615 = 1 - e^{-0.000432 R}$$

$$R = 1496.52$$

Q6) 1. i) Heterogenous group as parameters vary by patient.

2. ii) a) $E(X) = 0.5 \times 0.1 + \frac{1}{3} \times 0.3 + \frac{1}{6} \times 0.9$

$$= 0.3$$

$$E(X^2) = 0.5 \times 0.1^2 + \frac{1}{3} \times 0.3^2 + \frac{1}{6} \times 0.9^2$$

$$= 0.17$$

$$V(X) = 0.17 - 0.3^2 = 0.08$$

b) $E(S/\lambda) = (\lambda m) \text{Var}(S_i/\lambda_i)$

$$= \lambda_i m_2$$

$$E(S_i) = E[E(S_i/\lambda_i)] = E(\lambda_i m_i)$$

$$= 0.3 m_1$$

$$= 0.3 \times 200$$

$$= 75$$

3. (ii) $\text{Var}(\lambda_i) = 0.5 (0.2^2 + 0.4^2) - 0.3^2 = 0.07$

$$E(\sum S_i) = n E(S_i) = 0.3 \times 100 \times 200 = 2000$$

$$V(\sum S_i) = 0.3 \times 100 \times 200 + 0.07 \times 100^2 \times 200^2$$

$$= 6246000$$

IV) doubt -

Q7) Claim $\sim \text{Poi}(50)$
 Amount $\approx 100X$

$$f(x) = \frac{3}{32} (6x - x^2 - 5) \quad \text{when } 1 < x < 5$$

$$= 0 \quad \text{otherwise}$$

(i) $E(100X)$

$$= 100 \times \frac{3}{32} \int_1^5 x (6x - x^2 - 5) dx$$

$$= 100 \times \frac{3}{32} \times \int_1^5 (6x^2 - x^3 - 5x) dx$$

$$= 100 \times \frac{3}{32} \left[\frac{6x^3}{3} - \frac{x^4}{4} - \frac{5x^2}{2} \right]_1^5$$

$$= \frac{300}{32} [31.25 + 0.25] = 300$$

$$\text{Var}(100X) = E(100X)^2 - [E(100X)]^2$$

$$E(100X)^2 = 100^2 E(X^2)$$

$$= 100^2 \times \frac{3}{32} \int_1^5 x^2 (6x^2 - x^3 - 5x) dx$$

$$= \frac{30000}{32} \left[\frac{6x^5}{5} - \frac{x^6}{6} - \frac{5x^3}{3} \right]_1^5$$

$$= 98000$$

$$\text{Var}(100X) = 8000$$

$$E(Y) = 0.3 \times 200$$

$$= 60$$

$$V(Y) = 0.3 \times 200^2 - (60)^2$$

$$= 8400$$

$$Z = X + Y$$

$$E(Z) = E(X) + E(Y) \text{ as } X \text{ \& } Y \text{ are independent}$$

$$= 360$$

$$V(Z) = \text{Var}(X + Y)$$

$$= \text{Var}(X) + \text{Var}(Y) \text{ as } X \text{ \& } Y \text{ are independent}$$

$$= 16400$$

$$E(S) = E(N) E(Z)$$

$$= 50 \times 360$$

$$= 18000$$

$$V(S) = E(N) \text{Var}(Z) + \text{Var}(N) E(Z)^2$$

$$= 50 \times 16400 + 50 \times 360^2$$

$$= 7300000$$