

$$\text{Ques 12)} \quad \sum x = 385.2 \quad \sum x^2 = 12666.58$$

$$(1) \quad \sum y = ~~1162.5~~ 1162.5 \quad \sum y^2 = 119026.9$$

$$\sum xy = 38191.41$$

$$S_{xx} = 301.66$$

$$S_{yy} = ~~6049.7125~~ 6409.7125$$

$$S_{xy} = 875.16$$

$$\hat{\beta} = 2.901147$$

$$\hat{\alpha} = 3.74818$$

$$\boxed{y = 3.74818 + 2.901147x}$$

$$(ii) \quad \hat{\sigma}^2 = \frac{1}{10} \left[S_{yy} - \frac{S_{xy}^2}{S_{xx}} \right]$$

$$= 387.0745$$

$$-2.228 \leq \frac{\hat{\beta} - \beta}{\hat{\sigma} \sqrt{S_{xx}}} \leq 2.228$$

$$\hat{\beta} - 2.228 \frac{\hat{\sigma}}{\sqrt{S_{xx}}} \leq \beta \leq \hat{\beta} + 2.228 \frac{\hat{\sigma}}{\sqrt{S_{xx}}}$$

$$(0.377, 5.425)$$

S_{03} $F_{4,28}$ tabulated is 2.21

$\frac{5.19}{1.55}$

and our calculated value is 3.28

S_{03} we have sufficient evidence to reject H_0 .

So (c) H_0 : They are independent of each other.

Entered values H_a : They are dependent.

Paper cleaned	Salary			
	3-5	5-8	8-10	10-12
0-3	27.42	23.089	14.43	11.06.
4-6	15.15	12.76	7.97	6.14
7-9	14.43	12.15	7.59	5.82.

$$\chi^2_{\text{cal}} = \frac{\sum (E_i - O_i)^2}{E_i}$$

$$\Rightarrow 11.27 + 0.4133 + 4.925 + 3.3204 + 4.384 + 4.1079 + 0.133 + 0.00319 + 6.162 + 1.4175 + 7.234 + 6.56$$

$$\Rightarrow \boxed{39.929}$$

$$\chi^2_6 = 12.592$$

Since $\chi^2_{\text{cal}} > \chi^2_{\text{Tab}}$ hence we have sufficient evidence to reject H_0 .

Examining $\bar{y}_1 - \bar{y}_3 = 8$
 hence there is a significant diff. blue means 1 & 3
 sig.

Sol (4) (i) Already in Sol (3) (ii)

(iii) ~~For~~ $H_0: \mu_1 = \mu_2 = \dots = \mu_5$
 H_a : at least one of the mean is not same

$$\frac{T^2}{N} = \frac{(\sum y_1 + \sum y_2 + \sum y_3 + \sum y_4 + \sum y_5)^2}{N} = 104385.9394$$

$$SS_{\text{Reg}} = \frac{(354)^2}{7} + \frac{(386)^2}{8} + \frac{(87)^2}{6} + \frac{(645)^2}{7} + \frac{(384)^2}{5} - \frac{T^2}{N}$$

$$= 22325.68917$$

$$SS_{\text{TOT}} = 69930.0606$$

$$SS_{\text{Res}} = SS_{\text{TOT}} - SS_{\text{Reg}}$$

$$= 47604.37143$$

ANOVA		df	SS	MS	F
Source of variation					
Reg.		4	22325.69	5581.4225	3.28
Res		28	47604.3143	1700.154	
Total		33	69930.0606		

(iii) H_0 : The mean diff. is same for each city

H_0 : The mean diff are not same.

$$SS_T = 1495 - \frac{103^2}{28} = 1116.11$$

$$SS_B = \frac{1}{7} \left(64^2 + 44^2 + 8^2 + (-13)^2 \right) - \frac{103^2}{28} = 516.11$$

$$SS_R = SS_T - SS_B = 600.00$$

ANOVA

Source	df	SS	MS	F
Treatments	3	516.11	172.04	6.88
Residual	24	600.00	25.00	
Total	27	1116.11		

Under H_0 : $f = \frac{172.04}{25} = 6.88$ using $F_{3,24}$ distribution

The 5% critical point is 3.009, so we have sufficient evidences to reject H_0 .

iv) Since: $\bar{y}_1 = 9.14$ $\bar{y}_2 = 6.29$ $\bar{y}_3 = 1.14$ $\bar{y}_4 = -1.14$

$$\bar{y}_1 > \bar{y}_2 > \bar{y}_3 > \bar{y}_4 \quad ; \quad s^2 = \frac{SS_R}{n-k} = 25$$

$$C_{24, 0.05} \cdot s \cdot \sqrt{\left(\frac{1}{7} + \frac{1}{7}\right)} = 2.064 \cdot \sqrt{25} \cdot \sqrt{\frac{1}{7} + \frac{1}{7}} = 5.52$$

$$\bar{y}_1 - \bar{y}_2 = 2.85, \quad \bar{y}_2 - \bar{y}_3 = 5.15, \quad \bar{y}_3 - \bar{y}_4 = 3$$

$\bar{y}_1 - \bar{y}_4 = 8$ observing that all 3 differences

are less than 5.52, we can say they have no significant difference.

$$\text{bii)} \quad \hat{\mu}_0 = 119.794$$

$$SE(\hat{\mu}_0) = 10.5989$$

95% Confidence Interval of μ_0 .

$$\Rightarrow 119.794 \pm 2.228 (10.5989)$$

$$\Rightarrow 119.794 \pm 23.6144$$

$$\Rightarrow (96.17956, 143.4084)$$

Sol (3) (i) Comments on Plot :

- The centres of distributions differ for all four cities. Thus there's a prima facie case for suggesting the underlying means are different.
- The difference b/w mean time taken to communicate to office in peak hours & non peak hours are in order City A, City D [highest, lowest].

(ii) Assumptions

- The Population must be normal.
- The Population must have a common variance.
- The observations are independent.

Probability & stats

Assignment

$$\text{Sol ① } \sum x^2 = 92500 ; \bar{x} = 85$$

$$\sum y^2 = 372717 ; \bar{y} = 173.7$$

$$\sum xy = 182560$$

$$S_{xx} = \frac{\sum x_i^2 - n(\bar{x})^2}{n} \Rightarrow 20250$$

$$S_{yy} = \frac{\sum y_i^2 - n(\bar{y})^2}{n} \Rightarrow 71000.1$$

$$S_{xy} = \frac{\sum xy - n(\bar{x}\bar{y})}{n} \Rightarrow 34915.$$

$$(a) \beta = \frac{S_{xy}}{S_{xx}} = 1.7242.$$

$$\alpha = \bar{y} - \beta \bar{x} \Rightarrow 27.143.$$

$$\text{So, } \hat{y} = 27.143 + 1.7242 x$$

(b) gradient is no. of hours he spend in A
upon amount withdrawn.